



S+ SimulationsPlus

BO Session C : Modeling approaches to integrate dissolution in PBBMs

M-CERSI workshop

2023 August 29

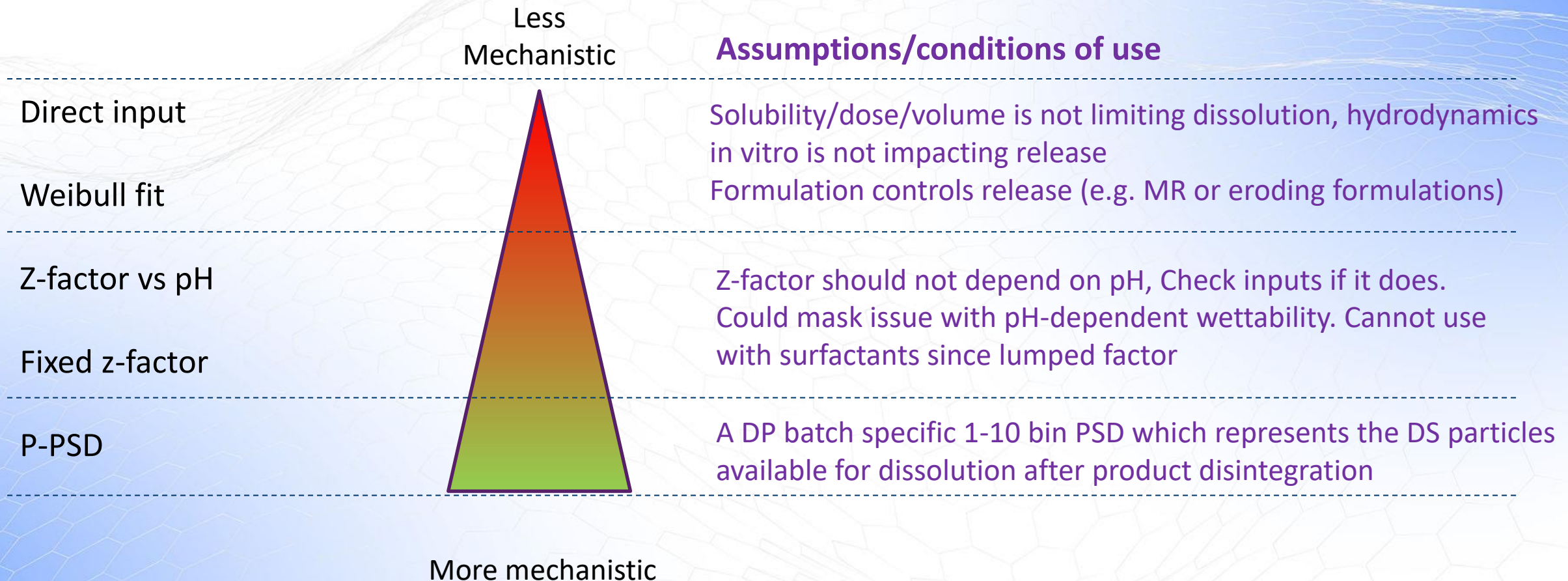


Outline

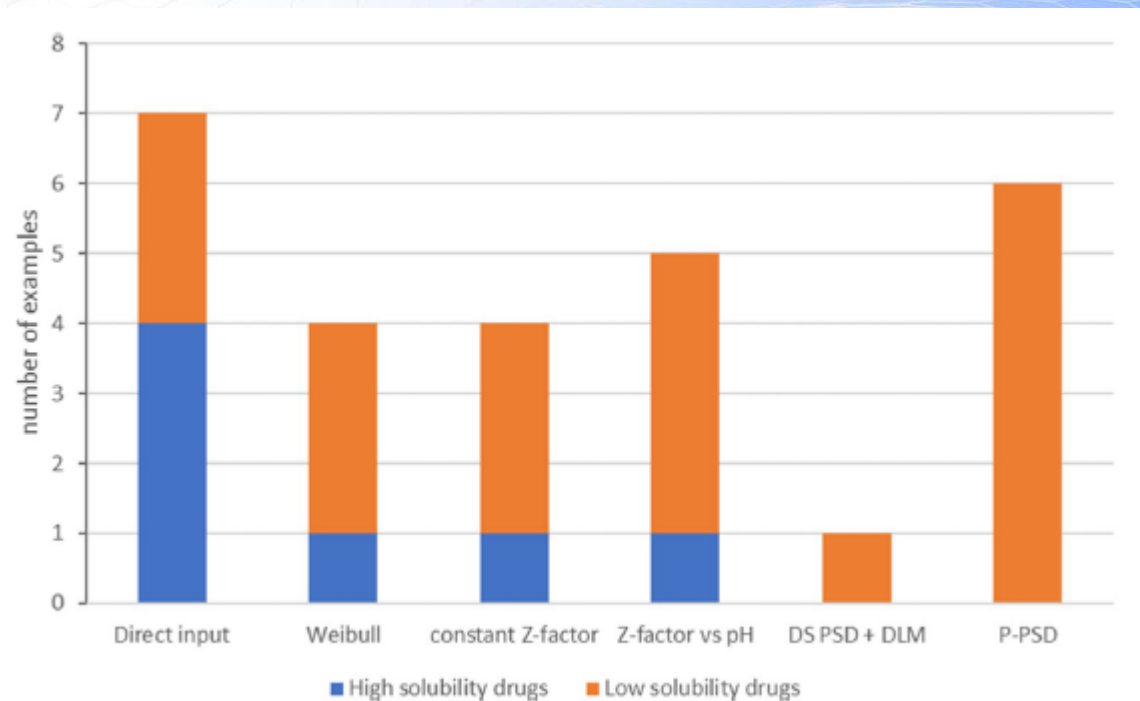
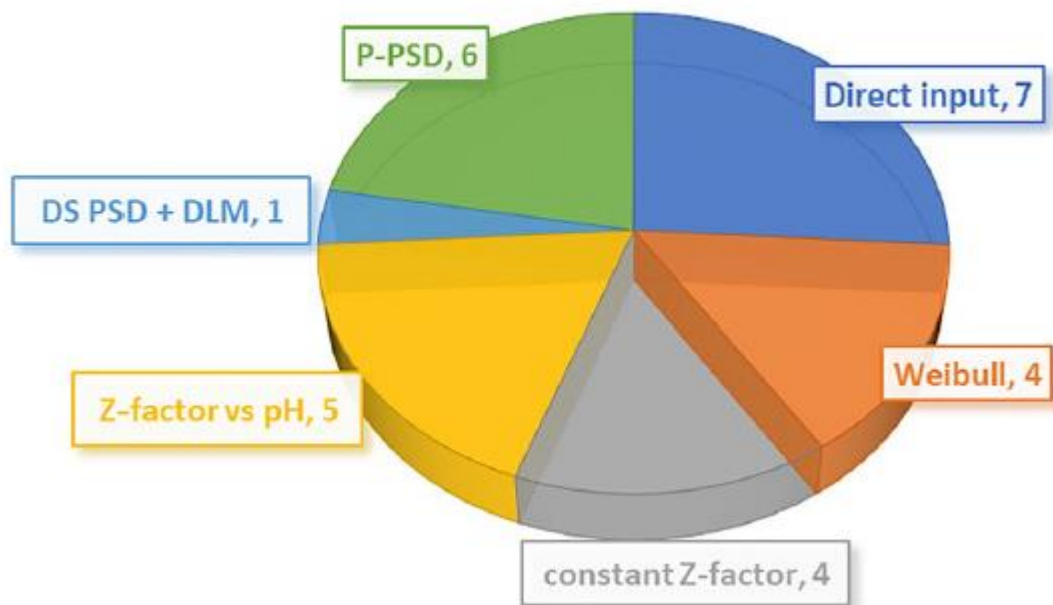


- Different models to fit dissolution
 - Assumptions for each model
 - Use for IR formulation fitting
 - Main equations
- Important drivers of dissolution
 - How DS and DP CQAs can influence shape of profile
- How to choose a dissolution method and how to choose fitting strategy ?
- Take home messages

Dissolution integration: How methods compare



IR Dissolution integration: literature

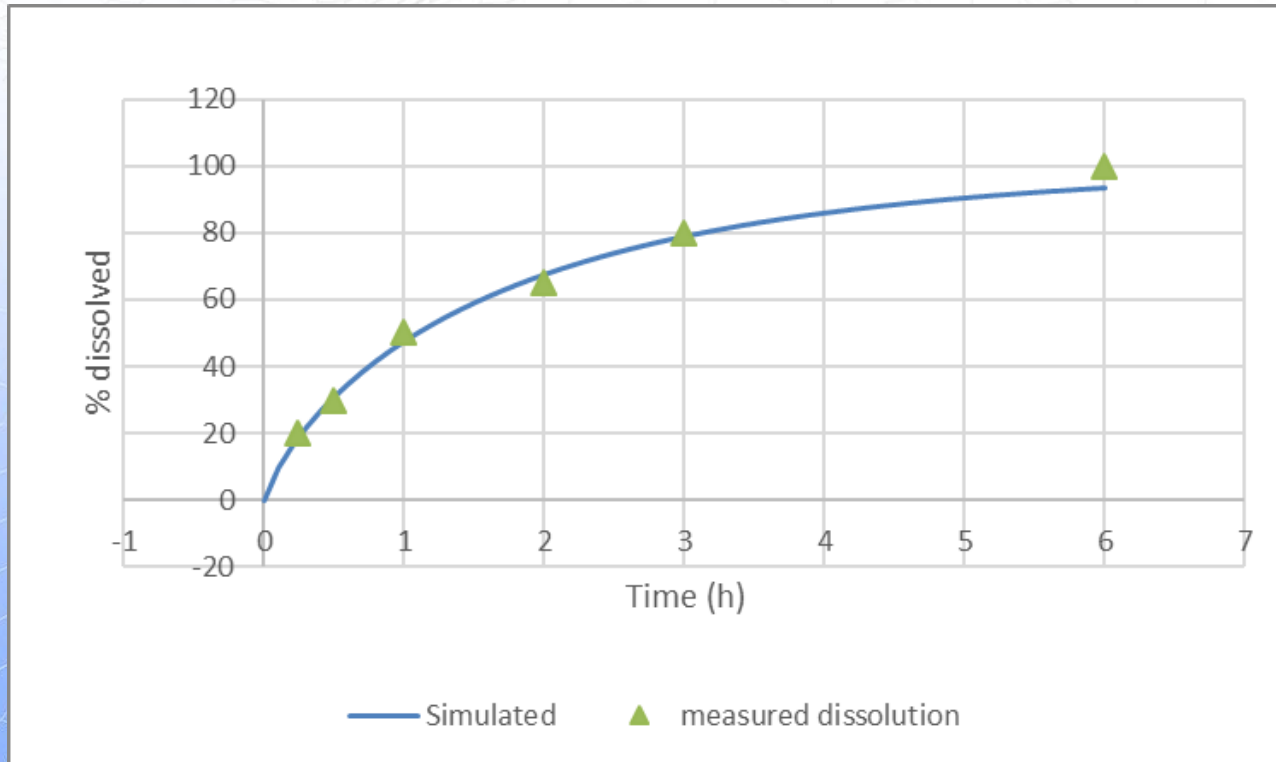


(1) Anand, O.; Pepin, X. J. H.; Kolhatkar, V.; Seo, P. The Use of Physiologically Based Pharmacokinetic Analyses—in Biopharmaceutics Applications - Regulatory and Industry Perspectives. *Pharmaceutical Research* **2022**. DOI: [10.1007/s11095-022-03280-4](https://doi.org/10.1007/s11095-022-03280-4).

Weibull equation

>V9.7 : up to three phase-Weibull

$$P\%(t) = P_{\max} \times \left(1 - \exp\left(-\frac{(t - t_{\text{lag}})^b}{A} \right) \right)$$



Max % dissolved	100
Lag time (h)	0
A parameter	1.54986
b parameter	0.799337
t1/2diss (min)	66
t80%diss (min)	188



Simple to fit to dissolution data
With 3 phases all profiles matched
Fill missing points



Is not mechanistic.
Imposes release over time

Z-factor-Takano

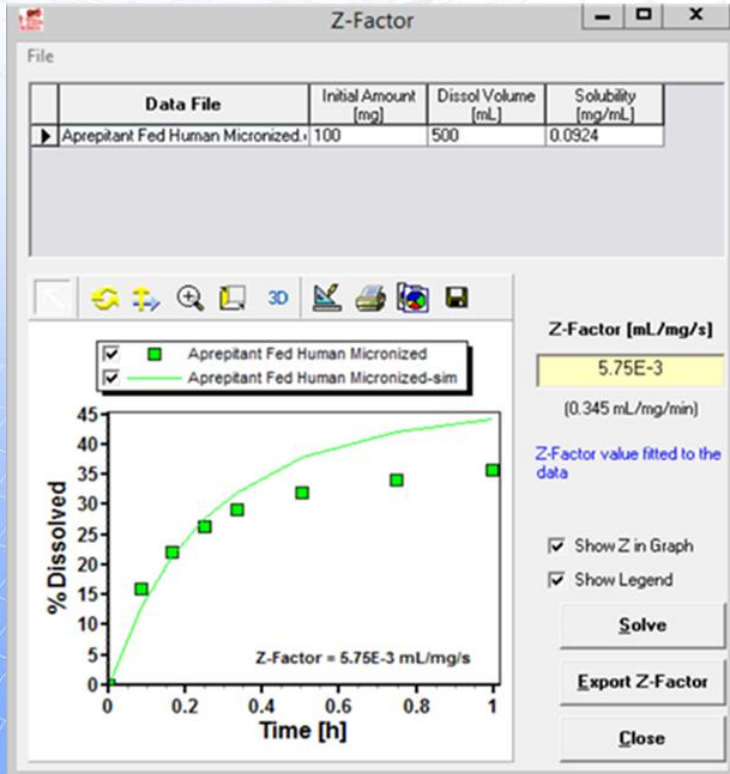
Takano, R., et al. (2006). "Oral absorption of poorly water-soluble drugs: computer simulation of fraction absorbed in humans from a miniscale dissolution test." Pharm Res 23(6): 1144-1156.

$$\frac{dX_{d,vitro}(t)}{dt} = \frac{3D}{\rho hr_0} \times X_{0,s,vitro} \times \left(\frac{X_{s,vitro}(t)}{X_{0,s,vitro}} \right)^{2/3} \times \left(C_s - \frac{X_{d,vitro}(t)}{V_{vitro}} \right)$$

$$= z \times X_{0,s,vitro} \times \left(X_{s,vitro} \times \left(\frac{X_{s,vitro}(t)}{X_{0,s,vitro}} \right)^{2/3} \times \left(C_s - \frac{X_{d,vitro}(t)}{V_{vitro}} \right) \right)$$

$$z = \frac{3D}{\rho hr_0}$$

Z groups particle size, diffusion and thickness of UWL and drug density.



Simple to fit to dissolution data
Mechanistic (dose, pH, volume)

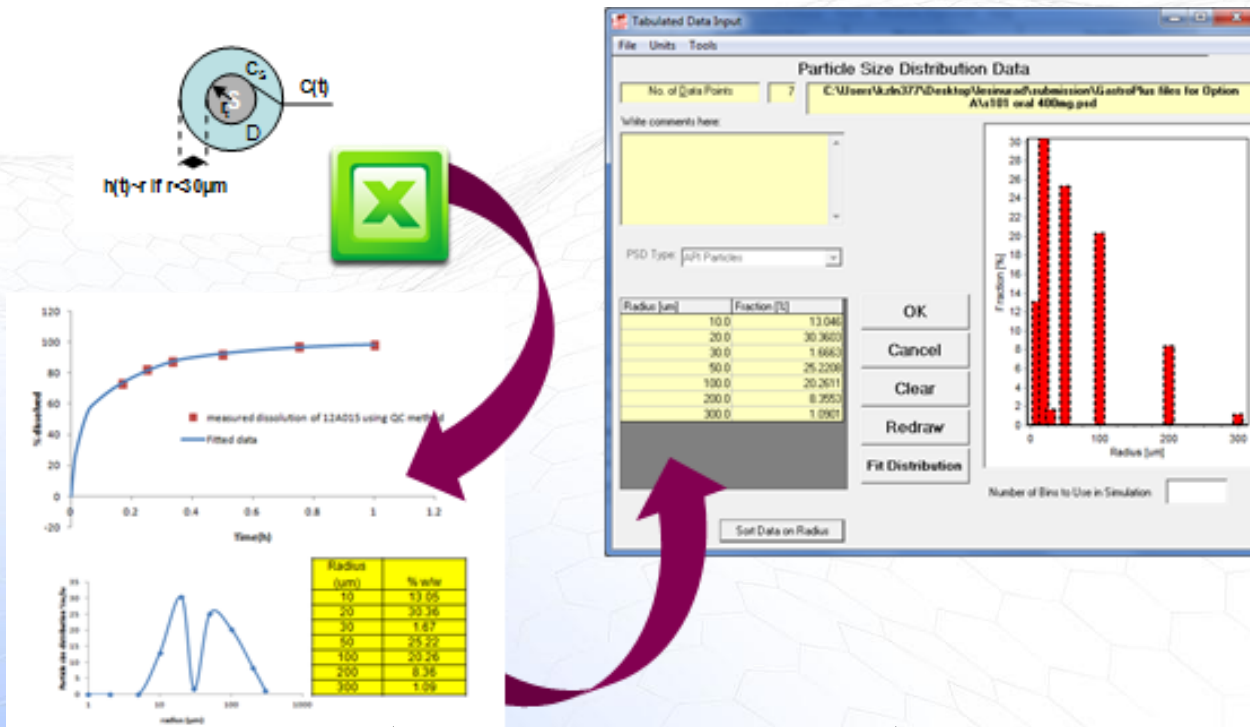


May not match all profiles (multimodal)



Cannot differentiate diffusion of micelles from free drug
Cannot integrate hydrodynamics over time
Particle size constant (OK for early stages)

P-PSD : Different tools available



1- Use of one dissolution data to extract the P-PSD

2- Verification that P-PSD is predictive of other dissolution conditions for same batch

3- Use of P-PSD as input in PBPK model

$$\frac{dm_{solid}}{dt} = -A(t) \times \left(f_u \times \frac{D_u}{h_u(t)} + \frac{1 - f_u}{f_u} \times \frac{D_b}{h_b(t)} \right) \times (C_{S,u} - C_u(t))$$

$$f_u = \frac{C_u(t)}{C(t)} \quad h_b = \sqrt[3]{\frac{D_b}{D_u}}$$



Simple to fit to dissolution data
Mechanistic (dose, pH, volume, surfactant)



Basic model comprises hydrodynamics with Johnson assumption

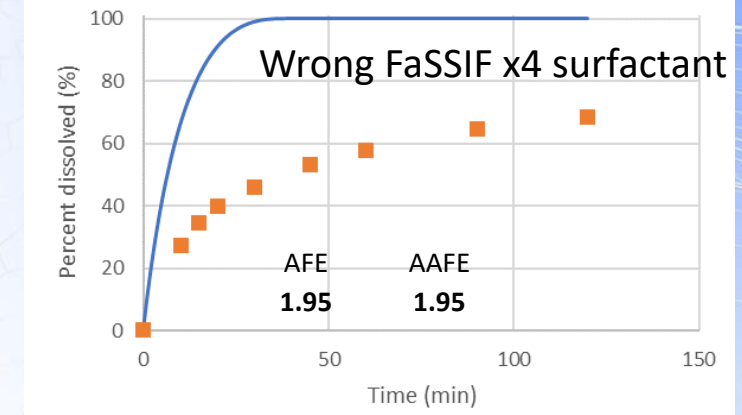
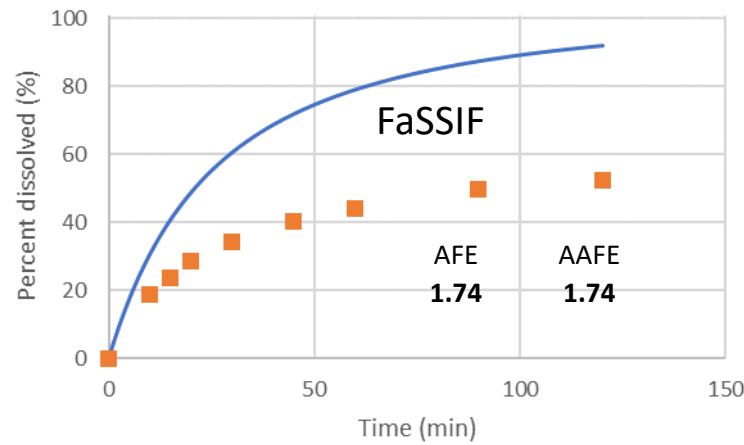
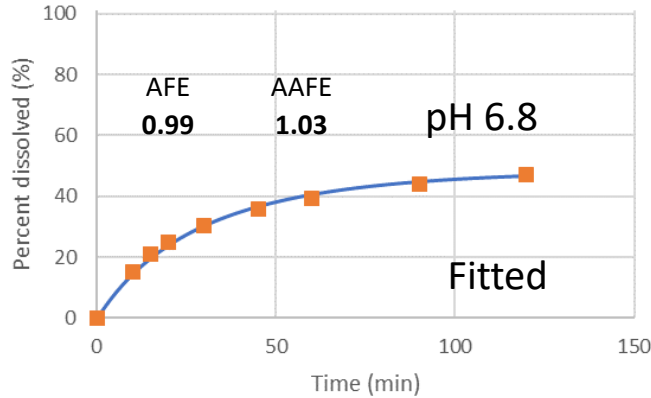
Commonalities and differences in dissolution fitting

Method	Equation	Comments	Reference
Noyes-Whitney (1897)	$\frac{dm_{solid}}{dt} = -A(t) \frac{D}{h} \times (C_S - C(t))$	UWL assumption around particles	https://www.ncbi.nlm.nih.gov/pubmed/16920290
Johnson (1989)	$\frac{dm_{solid}}{dt} = -\frac{D(1+2s)}{\rho hr_t s} \times (C_S - C(t)) \times m_{solid,t}$	Particles can be cylindrical	https://doi.org/10.1016/0378-5173(89)90069-0
Wang Flanagan (1999)	$\frac{dm_{solid}}{dt} = -\frac{3D}{\rho} \times \frac{1}{r_t} \times \left(\frac{1}{r_t} + \frac{1}{h}\right) (C_S - C(t)) \times m_{solid,t}$	Spherical particles only	https://doi.org/10.1021/js980236p
Takano (2006)	$\frac{dm_{solid}}{dt} = -\frac{3D}{\rho hr} \times m_{solid,0} \times \left(\frac{m_{solid,t}}{m_{solid,0}}\right)^{2/3} \times (C_S - C(t))$	Particle size constant during dissolution Lumped parameter which does not differentiate micelles	https://www.ncbi.nlm.nih.gov/pubmed/16715363
Gamsiz (2010)	$\frac{dm_{solid}}{dt} = -\frac{A(t)}{h} \times \left[D_u (C_{S,u} - C_u(t)) + D_b (C_{S,b} - C_b(t)) \right]$	Shrinking particles during dissolution Flux of unbound and bound drug explicit but same UWL	https://www.ncbi.nlm.nih.gov/pubmed/20963629
Pepin (2019)	$\frac{dm_{solid}}{dt} = -A(t) \times \left(f_u \times \frac{D_u}{h_u(t)} + \frac{1-f_u}{f_u} \times \frac{D_b}{h_b(t)} \right) \times (C_{S,u} - C_u(t))$ $f_u = \frac{C_u(t)}{C(t)}$ $\frac{h_b}{h_u} = \sqrt[3]{\frac{D_b}{D_u}}$	Shrinking particles Immediate partitioning of drugs to micelles at the surface Flux of unbound and bound drug explicit Different UWL for free and micelle bound drug Shrinking particles during dissolution	https://doi.org/10.1016/j.ejpb.2019.07.014

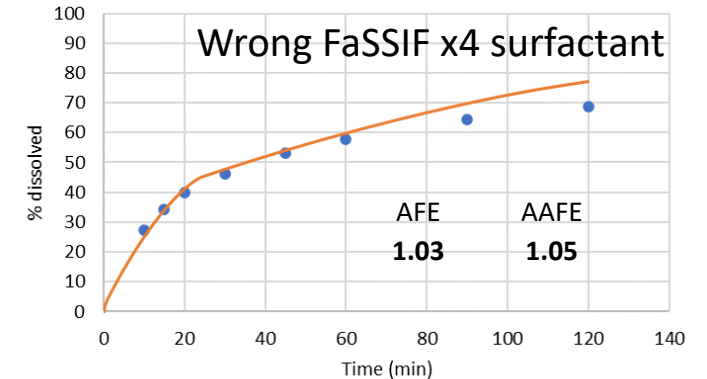
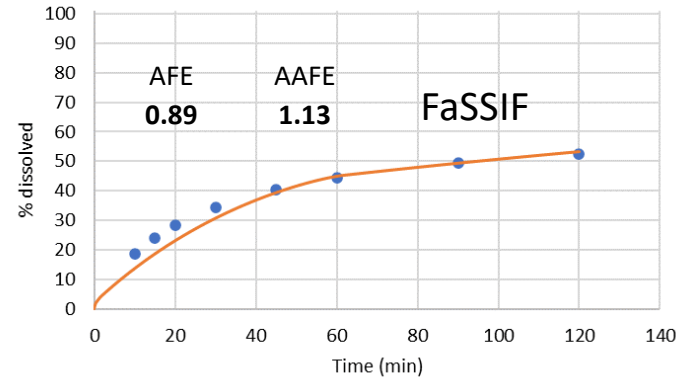
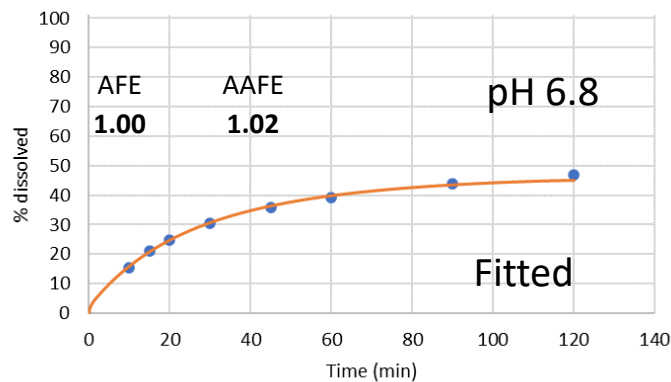
Z-factor vs P-PSD for surfactant media

Acalabrutinib capsule batch L0505009

Z-factor




P-PSD



Total apparent solubility in surfactant media + Z-factor fitted without surfactant → over-estimation of the dissolution rate
Diffusion coefficient is part of Z-factor but changes with medium micelle concentration

Outline

- Different models to fit dissolution
 - Assumptions for each model
 - Use for IR formulation fitting
 - Main equations
-  • Important drivers of dissolution
 - How DS and DP CQAs can influence shape of profile
- How to choose a dissolution method and how to choose fitting strategy ?
- Take home messages

Important drivers of Dissolution

Dissolution happens when there is a different chemical potential between the drug as a solid and the drug in solution = dynamics

$$\frac{dm_{solid}}{dt} = -A(t) \frac{D}{h} \times (C_s - C(t))$$

1897-Noyes-Whitney

<https://www.ncbi.nlm.nih.gov/pubmed/16920290>

Mass variation (kg.s^{-1})

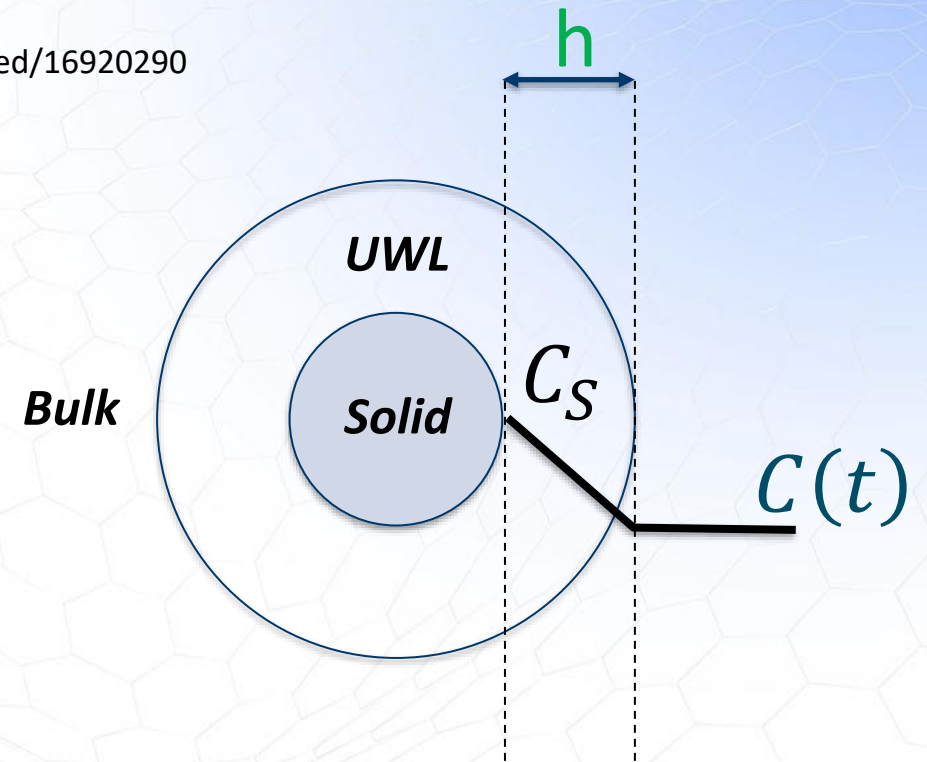
Surface area available for dissolution (m^2)

Diffusion coefficient ($\text{m}^2.\text{s}^{-1}$)

Thickness of the unstirred water layer (m)

Drug solubility (kg.m^{-3})

Drug concentration in the bulk of the medium (kg.m^{-3})



$A(t)$ Surface are available for dissolution

$$\frac{dm_{solid}}{dt} = -A(t) \frac{D}{h} \times (C_s - C(t))$$

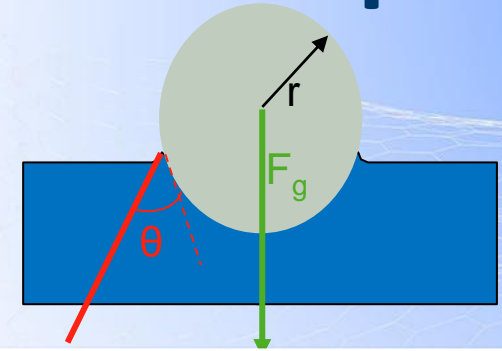
What surface to consider

- Capsule opening, tablet disintegration → Time correct data prior to fitting
- Wettability : pre-requisite
- → Excipients play a role to help the wetting (wicking and wetting agents help, lubricants or lipidic matrixes can delay wetting), wet granulation can improve wettability
- During dissolution surface changes with time as particles shrink
- Manufacturing process plays a role
 - Attrition can create more surface
 - Over-granulation or compression can “hide” drug inside granules

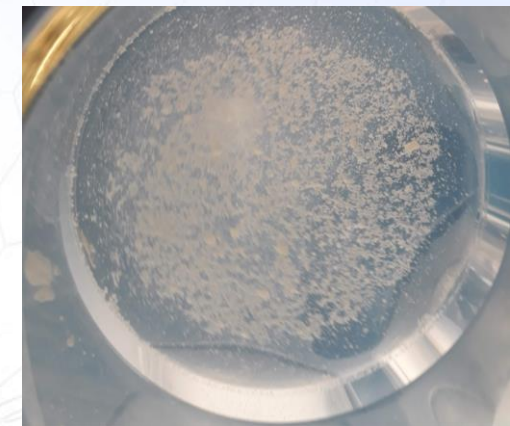
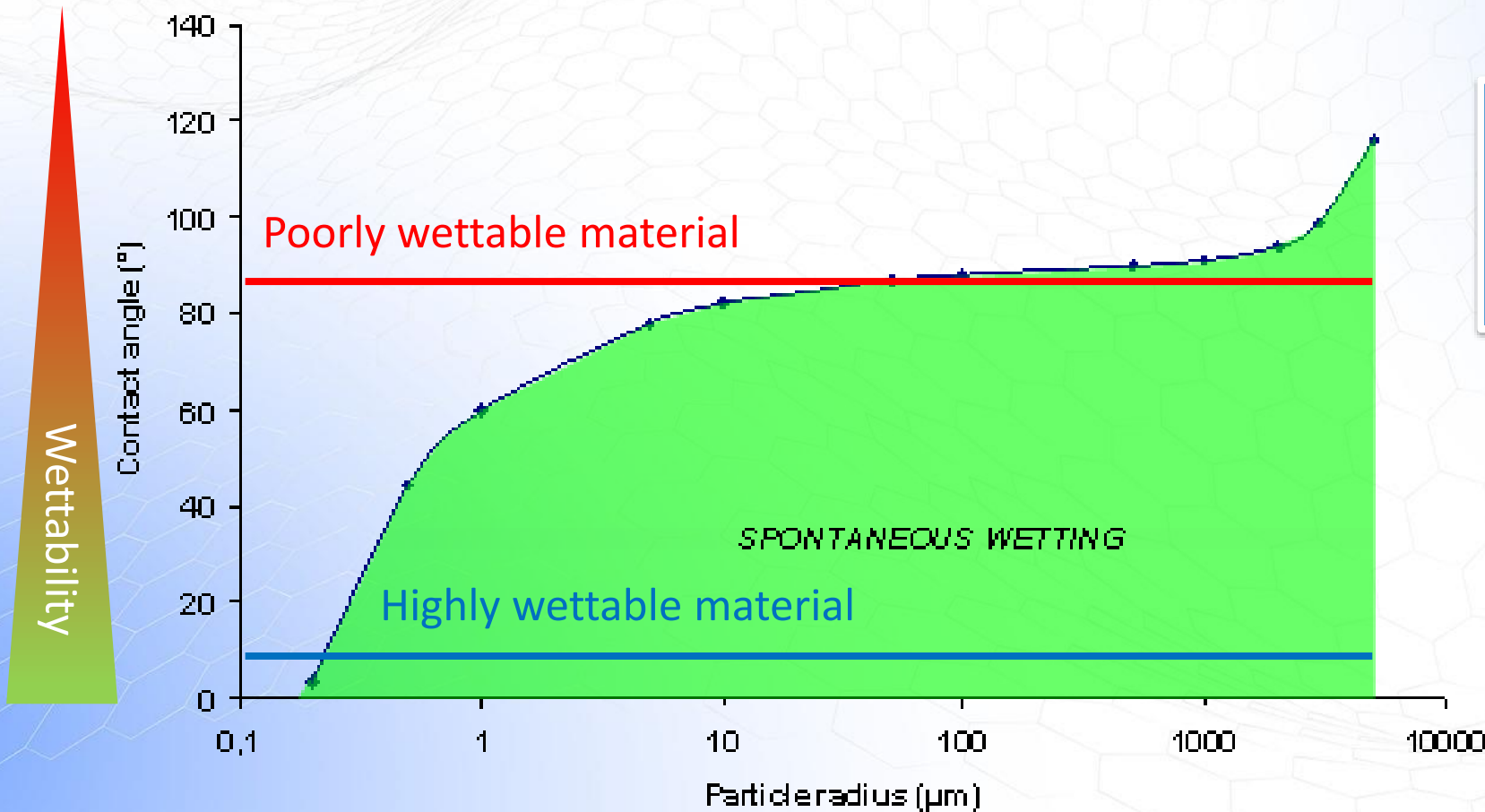
Difficult to predict DS particle size “available” for dissolution inside most solid dosage forms

Wettability of drugs : not all particles are equal !

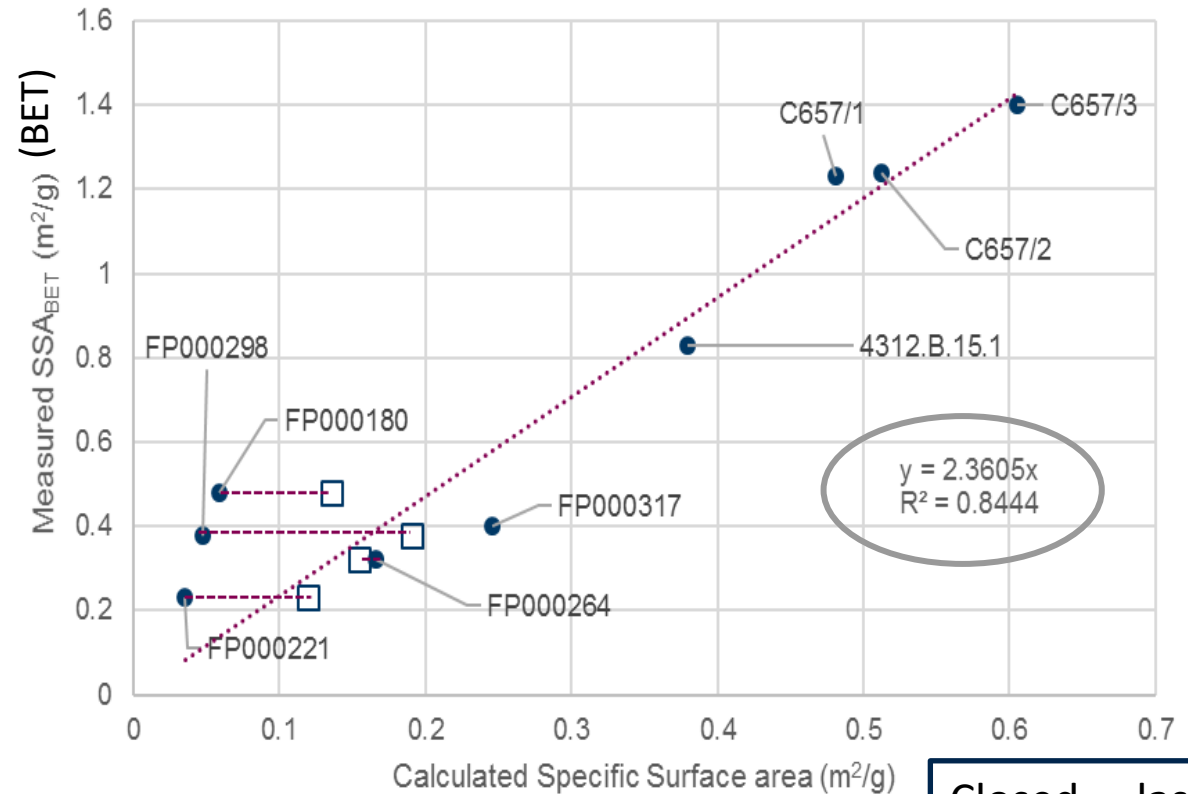
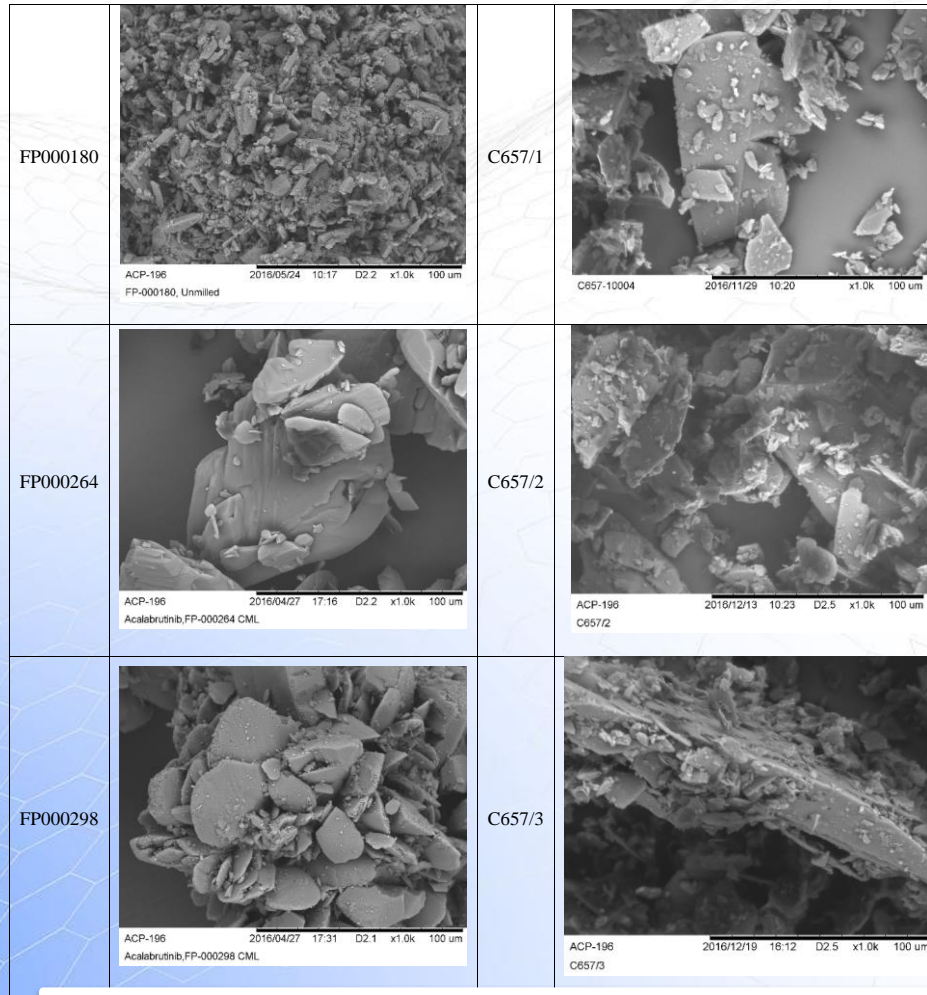
Limiting contact angle for spherical particle spontaneous wetting due to gravitation. $\rho_S = 1.2 \text{ g/mL}$, $\rho_L = 1 \text{ g/mL}$, $\eta_L = 1 \text{ mPa.s}$



Size of particles determines spontaneous wetting
Small particles wet less easily than large particles



Different measures of drug surface area

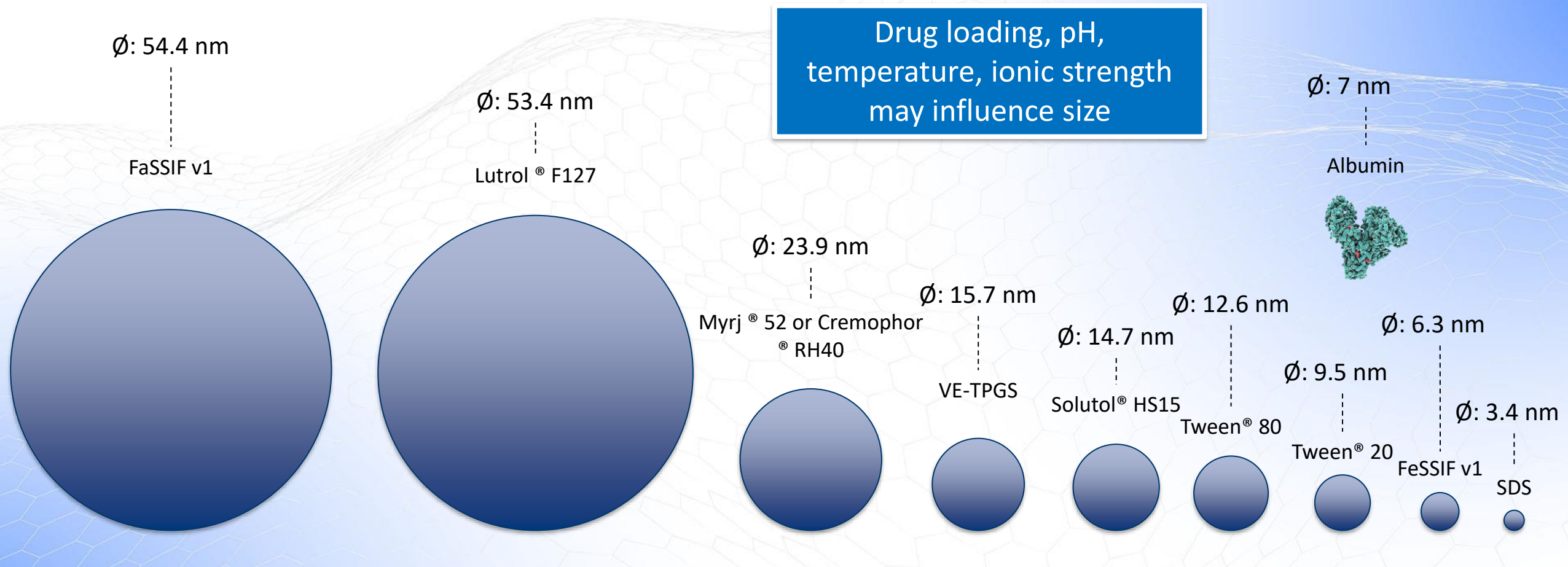


P-PSD shows “more” DS surface than laser diffraction

Closed = laser
Open = P-PSD (dissolution)

Laser under-estimates surface area esp. if particles are aggregated

Diffusion Coefficient – in vitro and in vivo micelles

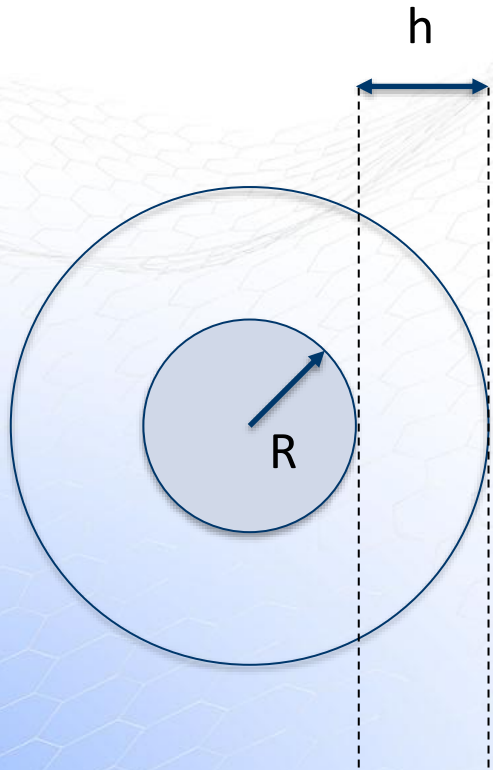


1. Nayem, J., et al., Micellar Morphology of Polysorbate 20 and 80 and Their Ester Fractions in Solution via Small-Angle Neutron Scattering. *Journal of Pharmaceutical Sciences*, 2020. 109(4): p. 1498-1508.
2. Okazaki, A., T. Mano, and K. Sugano, *Theoretical dissolution model of poly-disperse drug particles in biorelevant media*. *Journal of pharmaceutical sciences*, 2008. 97(5): p. 1843-52.
3. Hammouda, B., *Temperature Effect on the Nanostructure of SDS Micelles in Water*. *Journal of research of the National Institute of Standards and Technology*, 2013. 118: p. 151-67.
4. Feng, S., et al., *Predictive Modeling of Micellar Solubilization by Single and Mixed Nonionic Surfactants*. *J Pharm Sci*, 2018. 107(8): p. 2079-2090.

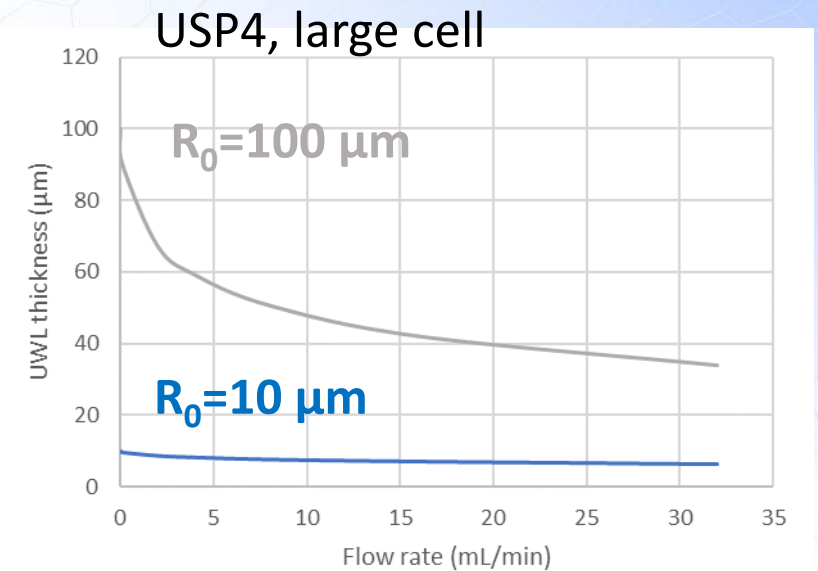
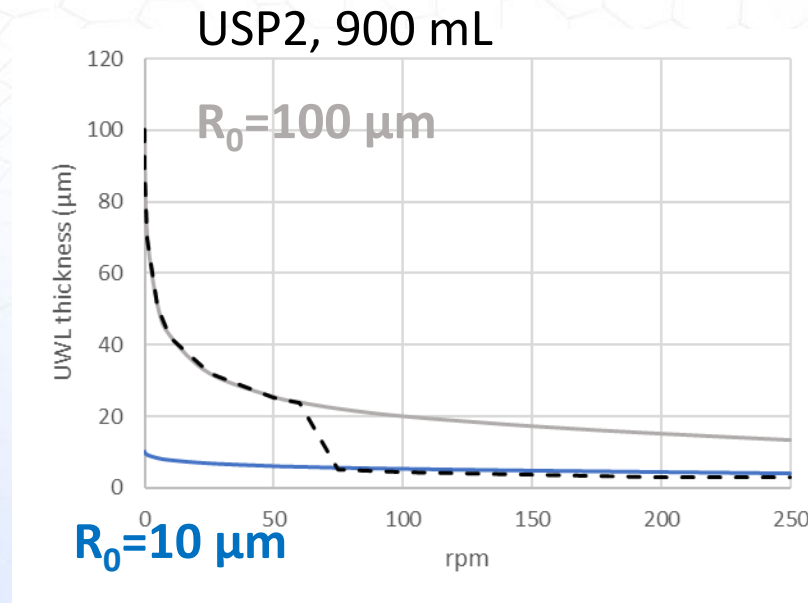
1.1 nm \varnothing unbound drug diffuses \approx 50 or 4 times faster than when bound to FaSSIF or SDS respectively

h Thickness of the unstirred water layer

$$\frac{dm_{solid}}{dt} = -A(t) \frac{D}{h} \times (C_s - C(t))$$



Default assumption $h=R_s$ up to $30 \mu\text{m}$ then constant if $R_s > 30 \mu\text{m}$ = low agitation conditions representative of in vivo hydrodynamics

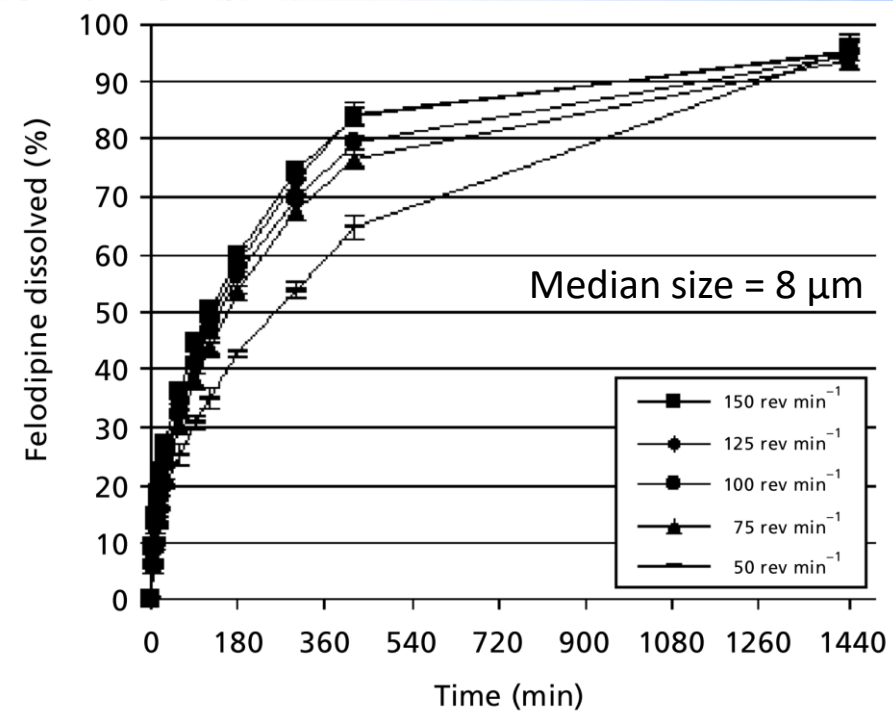
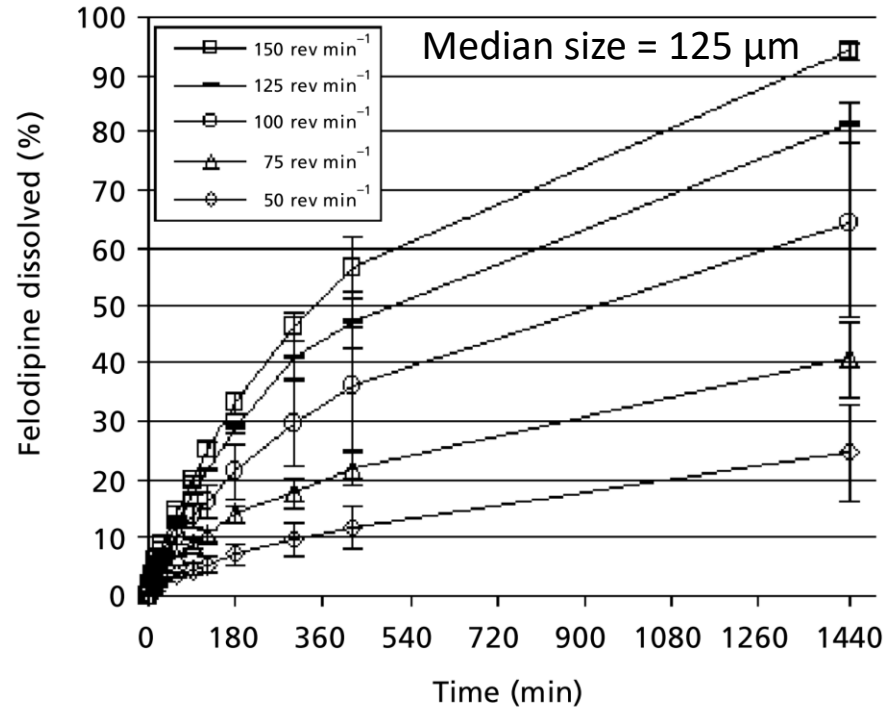


Hydrodynamics more important for large particles, e.g. pellets or eroding tablets

h Thickness of the unstirred water layer

$$\frac{dm_{solid}}{dt} = -A(t) \frac{D}{h} \times (C_s - C(t))$$

10 mg felodipine suspension dissolution in USP2. 500mL simulated canine chyme ^A



Fitting (or prediction) of coarse particle dissolution needs to integrate variable UWL as function of agitation

Check that agitation does not influence dissolution prior to fitting with any other model

A: Scholz, A., et al., Can the USP paddle method be used to represent in-vivo hydrodynamics? J Pharm Pharmacol, 2003. 55(4): p. 443-51.

C_S Drug solubility Surface pH: why is it important !

$$\frac{dm_{solid}}{dt} = -A(t) \frac{D}{h} \times (C_S - C(t))$$

Dissolution rate is influenced by the micro-environmental pH (surface pH) for drugs that ionize

- Below max pKa for bases
- Above min pKa for acids

In the bulk the pH is not changed (for large volumes)
 In the vicinity of the drug surface, during dissolution, the pH is altered when acid-base reactions take place. This local pH determines the surface solubility which drives dissolution rate

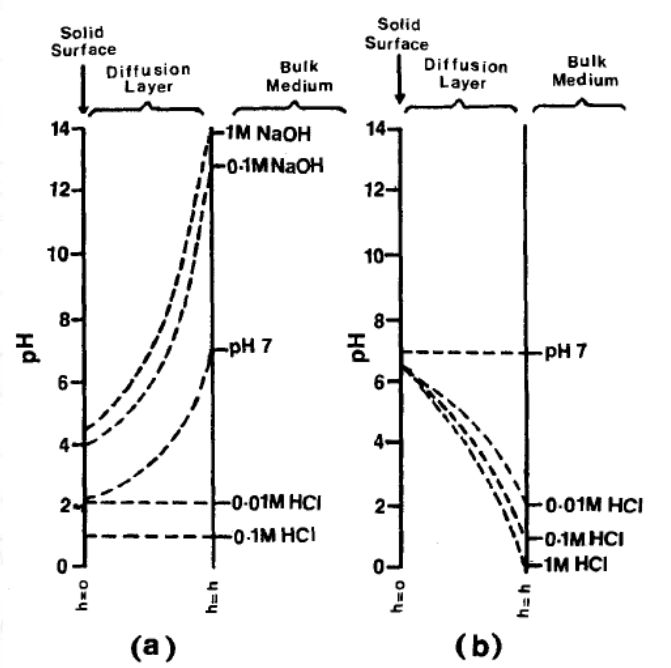
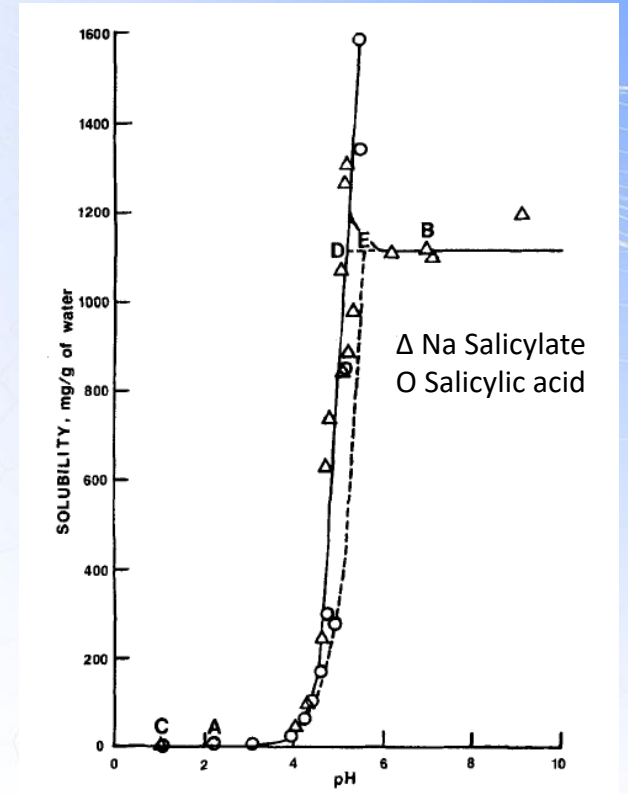
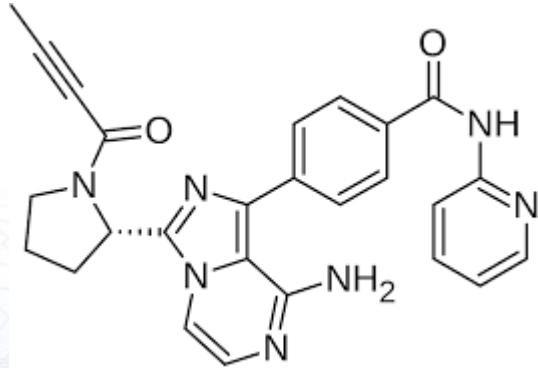


Figure 7—Graphical representations of the buffering effect of (a) salicylic acid and (b) sodium salicylate in the diffusion layers of various media. The dotted lines are schematic.



Serajuddin, A.T.M. and C.I. Jarowski, Effect of Diffusion Layer pH and Solubility on the Dissolution Rate of Pharmaceutical Acids and Their Sodium Salts II: Salicylic Acid, Theophylline, and Benzoic Acid. Journal of Pharmaceutical Sciences, 1985. 74(2): p. 148-154.

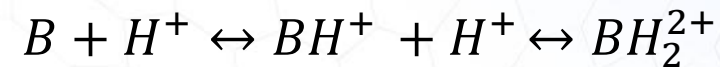
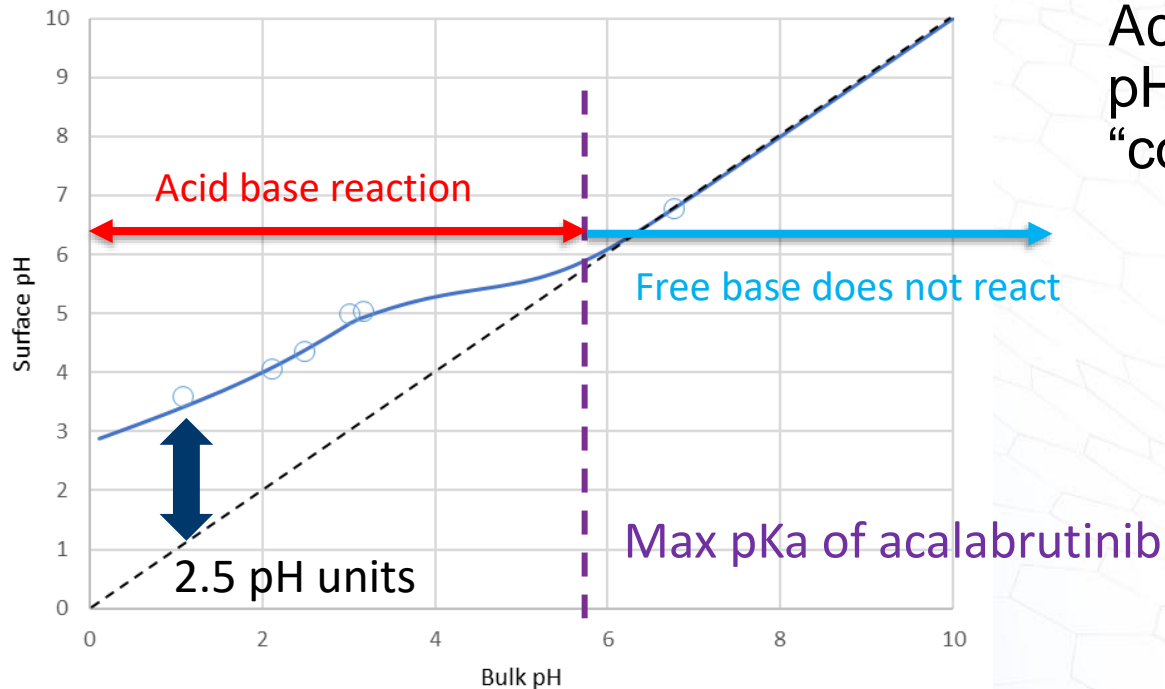
Example with acalabrutinib



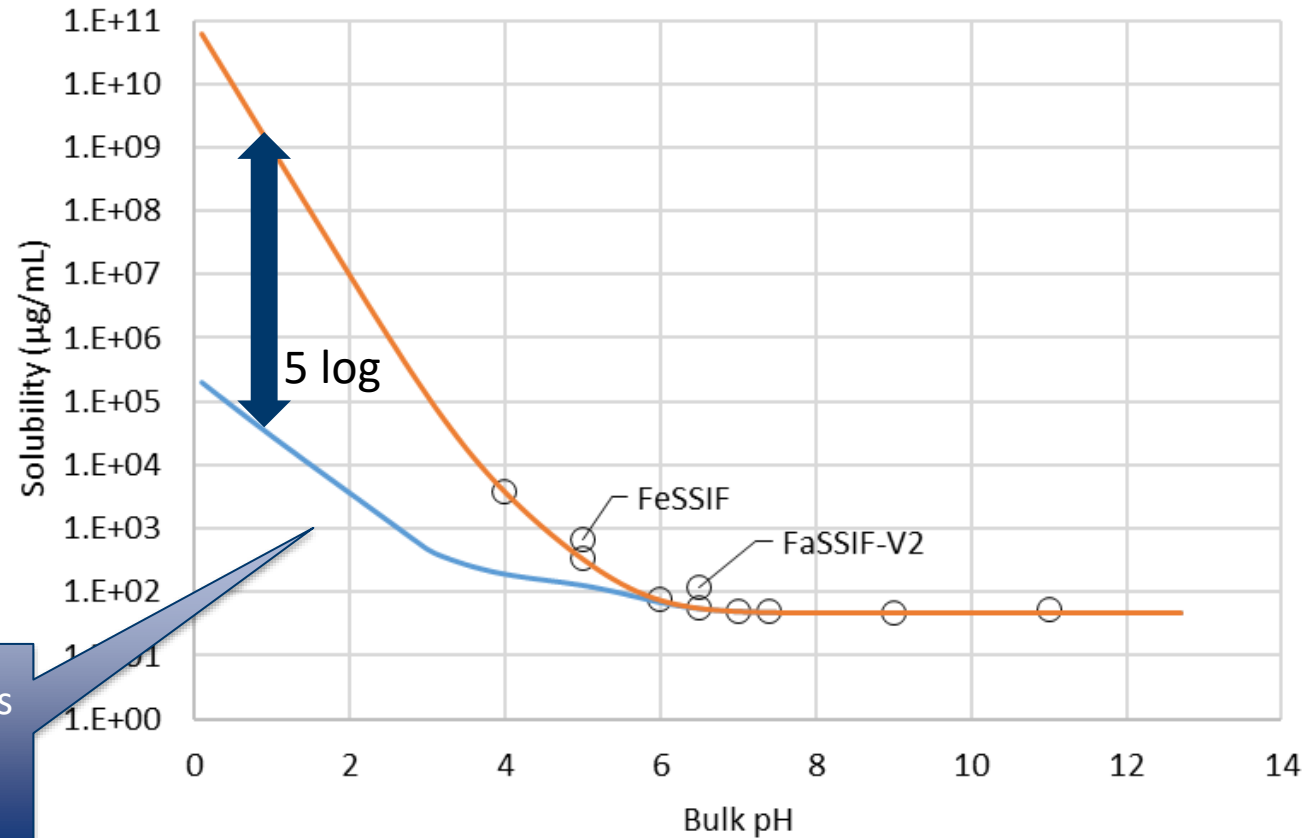
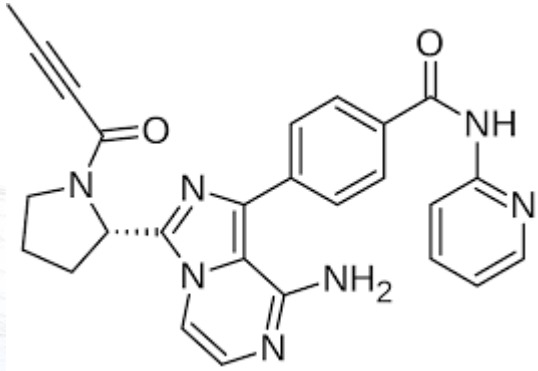
Acalabrutinib exhibits 2 pKas in the physiological range: 3.5(B), 5.8 (B)

Intrinsic solubility = 48 ug/mL @ pH 9

Acid base reaction at the surface : surface pH > bulk pH during dissolution below pKas since the free base “consumes” protons from the bulk to ionize.



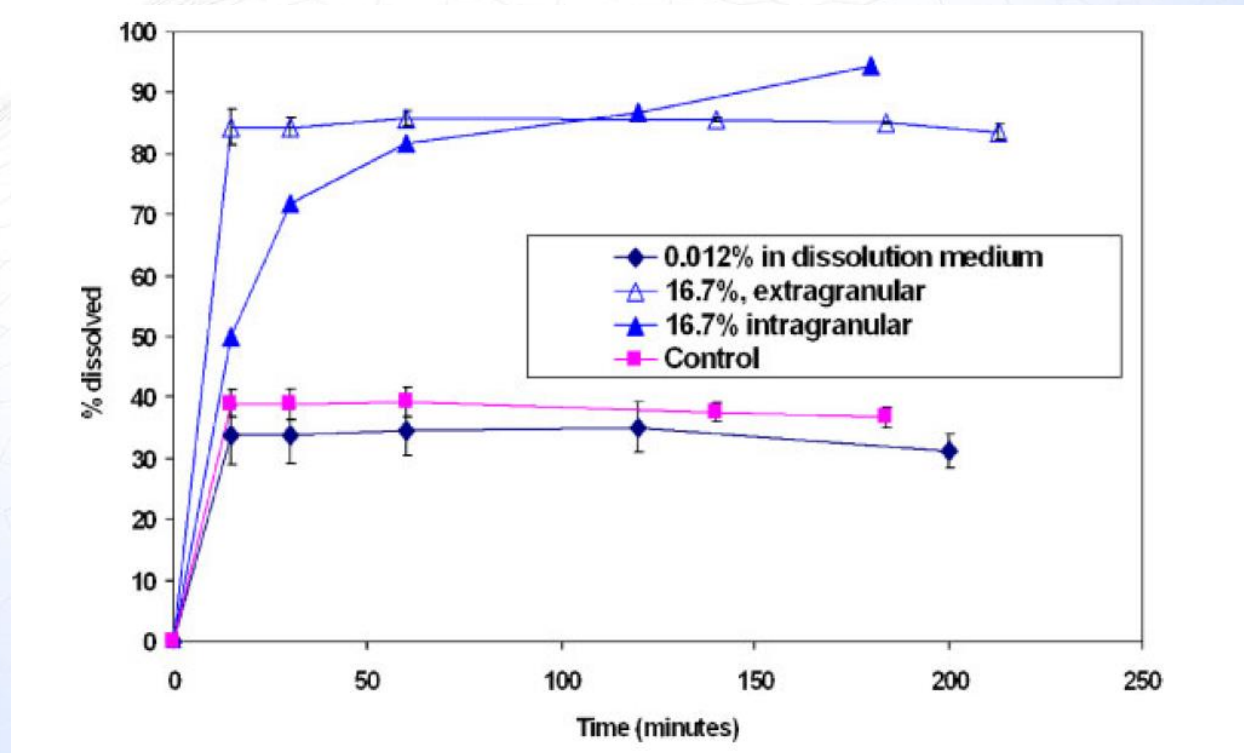
Surface vs bulk pH solubility profile



Surface solubility drives
in vitro and in vivo
dissolution

○ Measured — Surface sol µg/mL — Bulk sol µg/mL

Surface pH can be influenced by excipients



Effects of tartaric acid on the dissolution profile of BMS-561389 tablets in acetate buffer, pH 5.5

Badawy SIF, Gray D, Zhao F, Sun D, Schuster A, Hussain MA. 2006. Formulation of solid dosage forms to overcome gastric pH interaction of the factor Xa inhibitor, BMS-561389. Pharm Res 23: 989-996.

Bulk concentration

$$\frac{dm_{solid}}{dt} = -A(t) \frac{D}{h} \times (C_s - C(t))$$

Will determine the end of the dissolution if $C_s = C(t)$

Plateau < 100% dissolved if dose > $V \times C_s$



Plateau in dissolution does not always signify that an equilibrium is reached !

Plateau could hide :

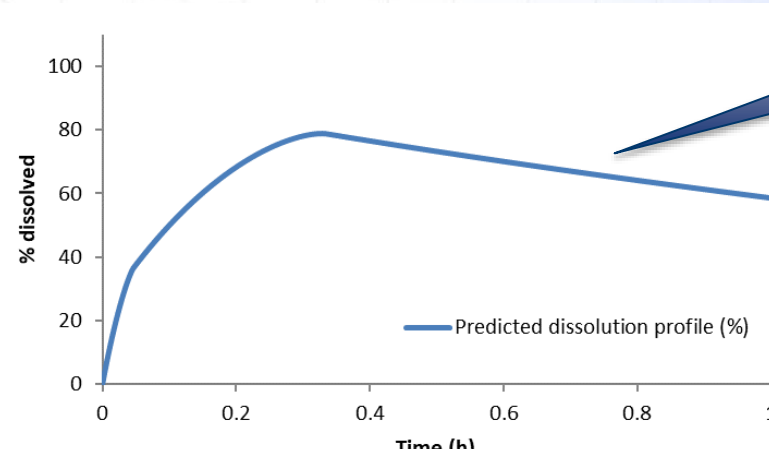
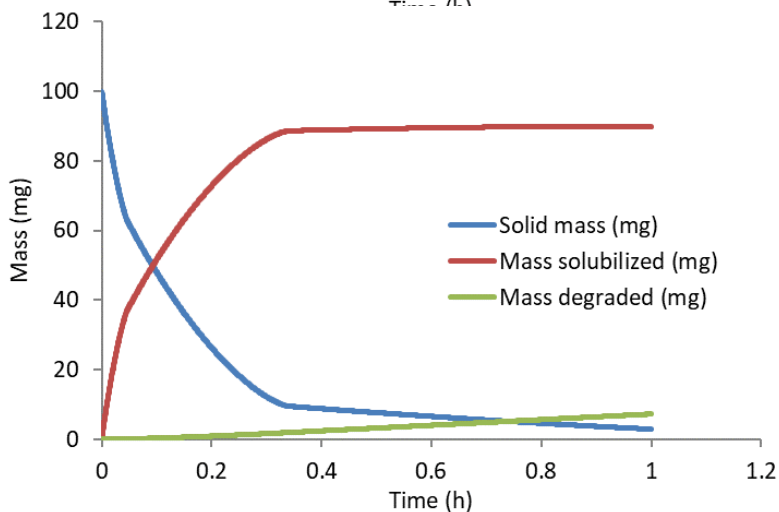
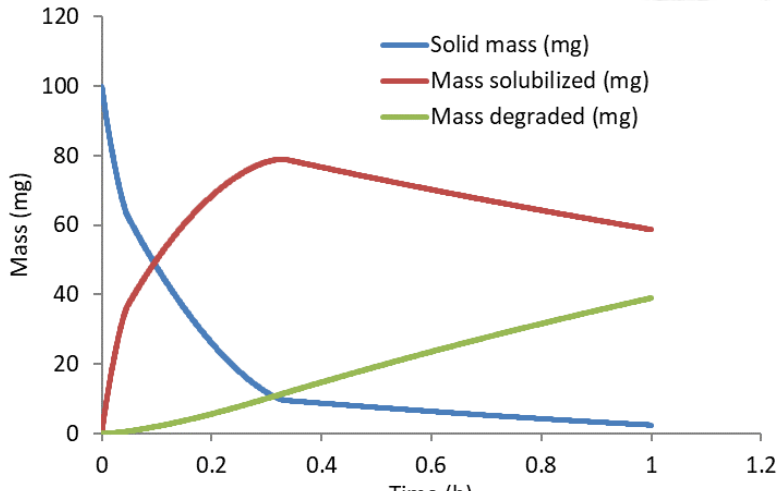
Chemical degradation

Presence of polymorphic impurity

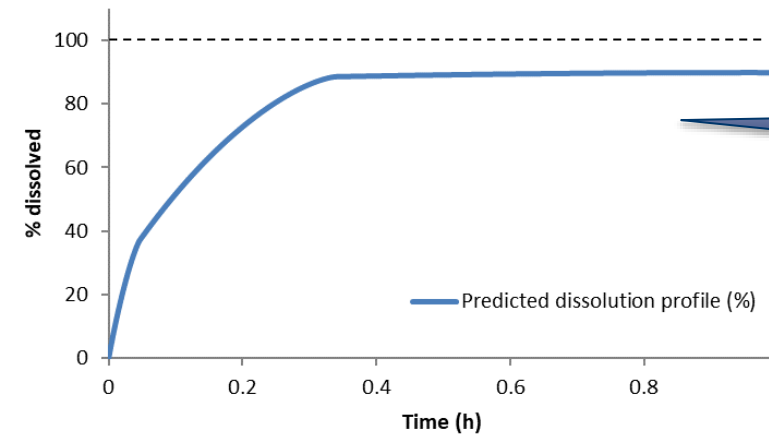
Precipitation

Impact of chemical degradation

Bulk concentration is decreased over time, e.g. Rifampicin + Isoniazid at pH 2

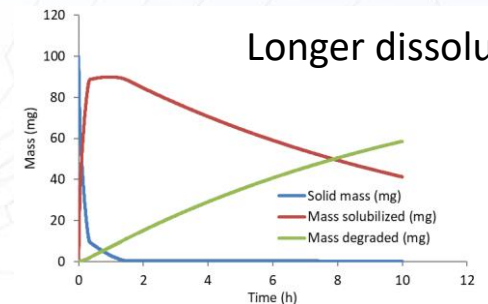


Rapid degradation = bell shape



This is not incomplete release

Slow degradation = plateau below 100%



Longer dissolution

Polymorph mixture

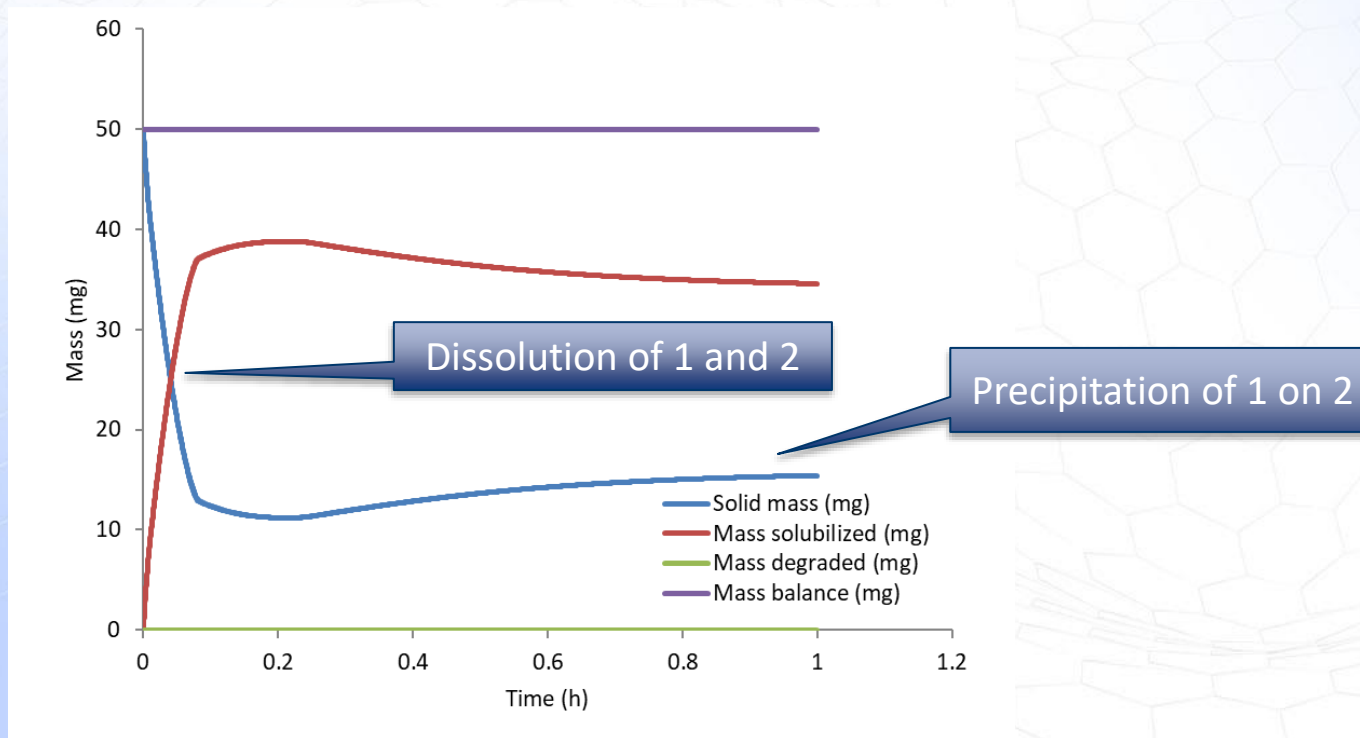
Two different solubilities C_{S1} , C_{S2} , same released moiety = same bulk concentration

$$\frac{dm_{solid}}{dt} = -A_1(t) \frac{D}{h} \times (C_{S1} - C(t)) - A_2(t) \frac{D}{h} \times (C_{S2} - C(t))$$

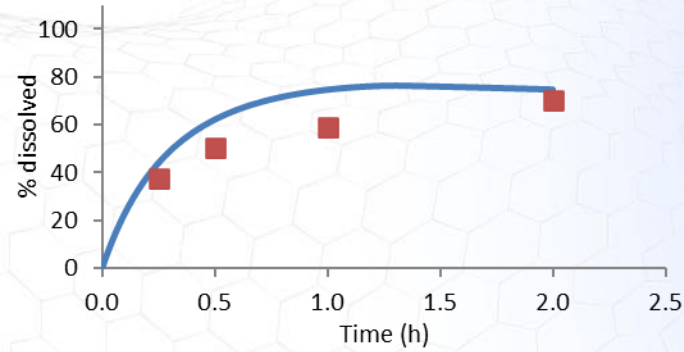
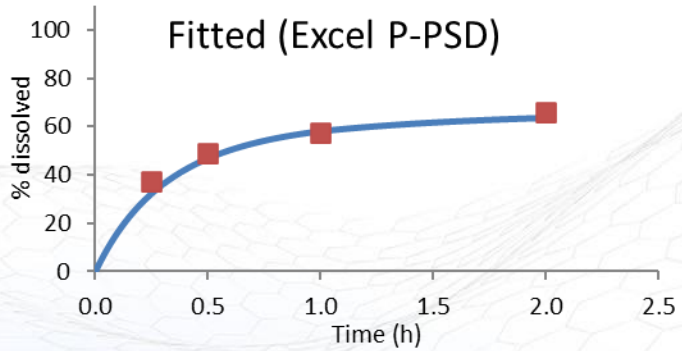
$$C_{S1} > C_{S2}$$

Polymorph 1 dissolves faster than polymorph 2

When $C_{S2} < C(t) < C_{S1}$ solute precipitates on polymorph 2

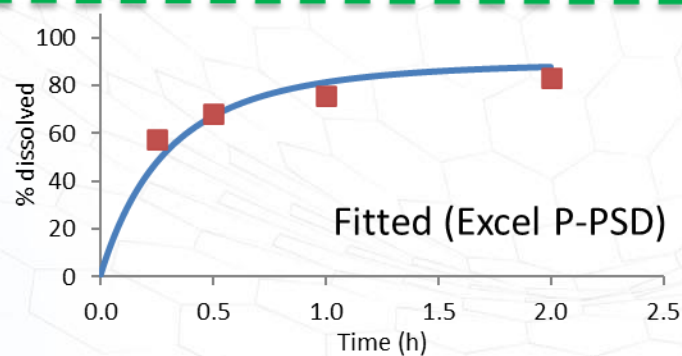
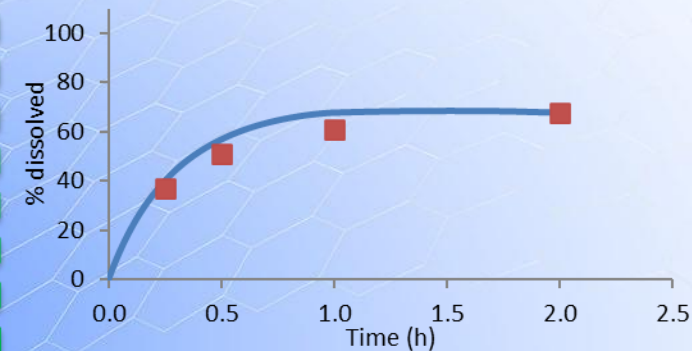
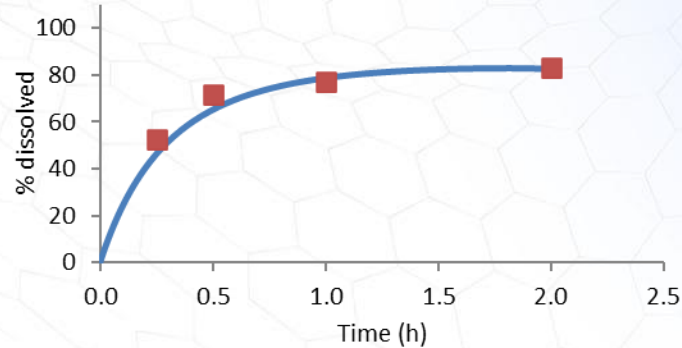
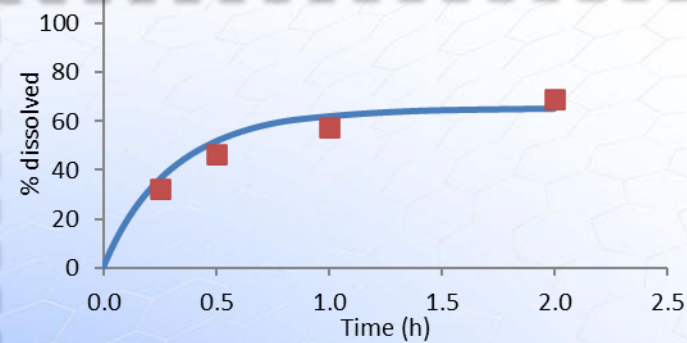


Rifaximin polymorph α and β mixtures ^A

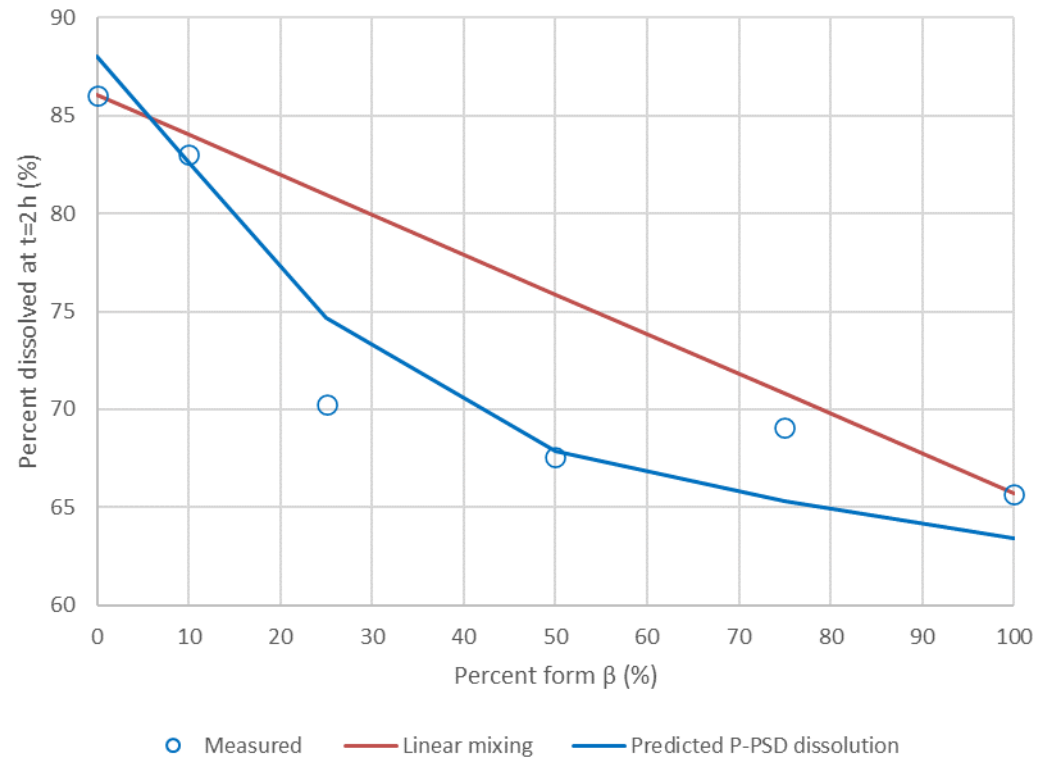


$$C_S \alpha \approx 1.7 \times C_S \beta$$

Predicted
Excel P-PSD




Mixing law for rifaximin α and β



Extent of dissolution for polymorph mixtures does not always show linear relationship with impurity content

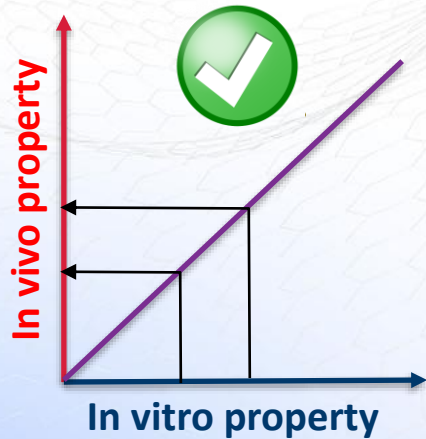
Outline

- Different models to fit dissolution
 - Assumptions for each model
 - Use for IR formulation fitting
 - Main equations
- Important drivers of dissolution
 - How DS and DP CQAs can influence shape of profile
-  How to choose a dissolution method and how to choose fitting strategy ?
- Take home messages

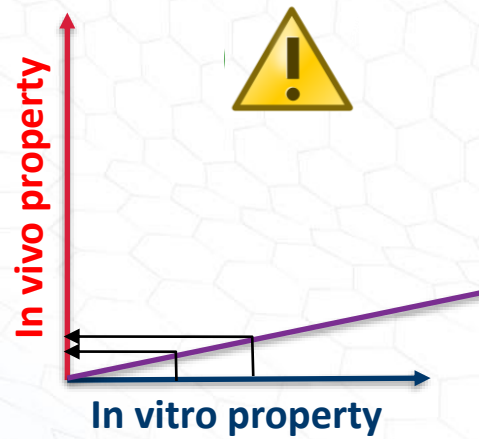
Choice of dissolution methods

Discrimination: changes in product in vitro performance are shown when CMA and or CPP are varied

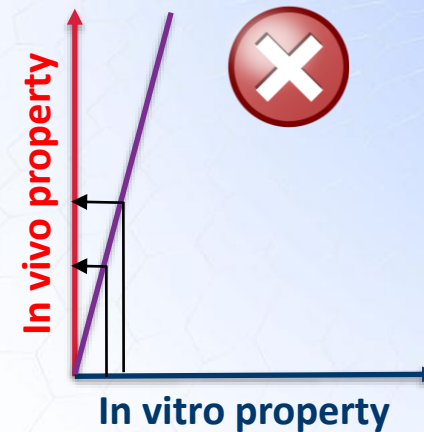
Rank order: Changes in product in vitro performance align with in vivo behaviour



Right level : changes of in vitro properties translate to in vivo performance



Over discriminative: large changes in vitro translate to smaller changes in vivo



Under discriminative: small changes in vitro translate to larger changes in vivo

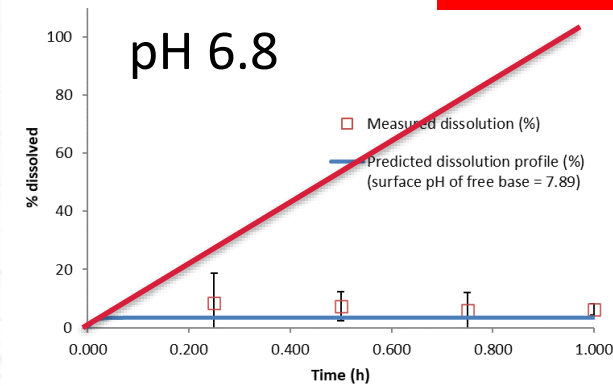
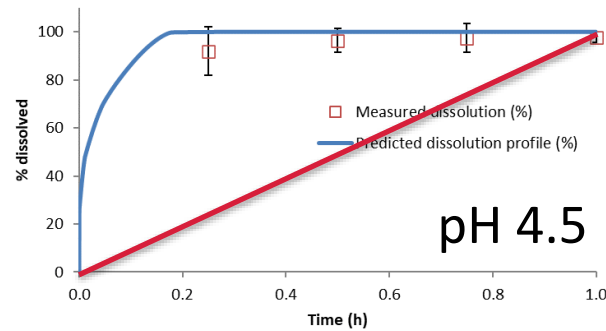
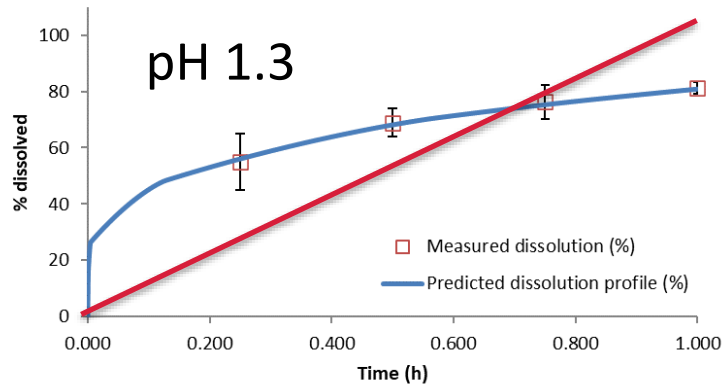
Both these methods may be clinically relevant and biopredictive

Choice of dissolution method for fitting

Choice of a discriminatory method

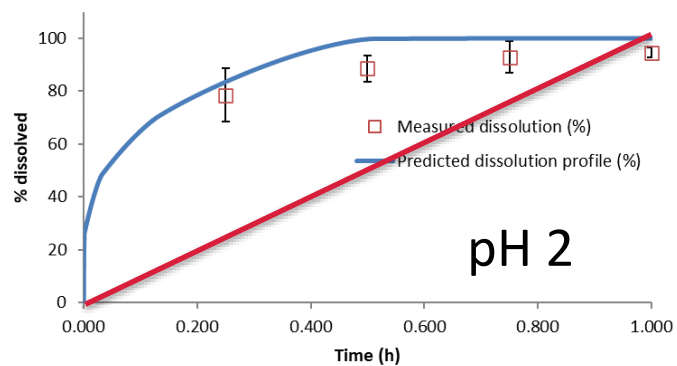
1-X method (Jesse Kuiper^A): Dose / Volume = solubility of the drug

20% < all points < 80% : best discrimination



All points below 20%
too low solubility = no
discrimination

All points above 80%
too high solubility = no
discrimination



1 point below 80%
not enough profile
definition

A: Abend, A., et al., Dissolution and Translational Modeling Strategies Enabling Patient-Centric Drug Product Development: the M-CERSI Workshop Summary Report. The AAPS journal, 2018. 20(3).

Excel P-PSD Typical inputs to calculate dissolution

2	Molecule			
3	Viscosity of water	μ_L	6.85E-04	Pa.s SF viscosity at T=..... 37
4	Unbound drug hydrated radius	r_h	5.48677E-10	m
5	Diffusion coefficient of unbound drug	D_u	6.0465580E-10	m ² .s-1
6	Avogadro n°	N_a	6.02214179E+23	-
7	Drug Molar weight	Mw	500	g/mol
8	True drug density	ρ_s	1.2	g/mL
9	Molecular volume	Mv	6.92E-28	m ³
10	Molar volume	MolV	4.17E-04	m ³
11	Boltzmann constant	k	1.3806504E-23	J.K-1
12	Gas constant	R_g	8.314472E+00	J.K-1.mol-1
13	Solubility in dissolution fluid w/o surfactants at at experiment temperature	$C_{s,u} @ T_{exp}$	0.48500	mg/mL or kg/m3 at T = 37
14	Melting point	T_m	473.15	K
15	Solubility in dissolution fluid w/o surfactants at at reference temperature	$C_{s,u} @ T_{ref}$	0.485	mg/mL or kg/m3 at Tref =..... 310.15
16	Tref for solubility	T_{ref}	310.15	K
17	Affinity for surfactant	k_{aff}	0.0818	mg/mL/mM
18	Concentration of surfactant in medium	C_{surf}	0	mM
19	Apparent solubility with surfactants	C_{total}	0.4850	mg/mL
20	Unbound fraction in solution	f_u	1	-
21	Micelle radius	r_{mic}	1.8	nm
22	Diffusion coefficient of micelle-bound drug	D_b	1.41254E-10	m ² .s-1
23	ratio of UWL thickness	h_b/h_u	0.615882306	
30				
31	Dissolution conditions			
32	Temperature	T	37	°C
33	Absolute Temperature	T	310.15	K
34	Drug mass administered	m_0	100	mg
35	Total dissolution time	t_{tot}	1	hours
36	Integration step	dt	0.9	seconds
37	number of steps	nsteps	4000	steps
38	Total volume of medium	V_L	900.0	mL
39	Degradation rate in solution	k_{deg}	0	min-1
40				

$$D = \frac{kT}{6\pi\eta R_h}$$

$$R_h = \sqrt[3]{\frac{3 \times M_w \times 10^{-23}}{4\pi N_A \rho_s}}$$

$$S_{app} = S_{sat} + k_{aff} \times C_{surf}$$

$$f_u = \frac{S_{sat}}{S_{app}}$$

The screenshot shows an Excel spreadsheet with the following content:

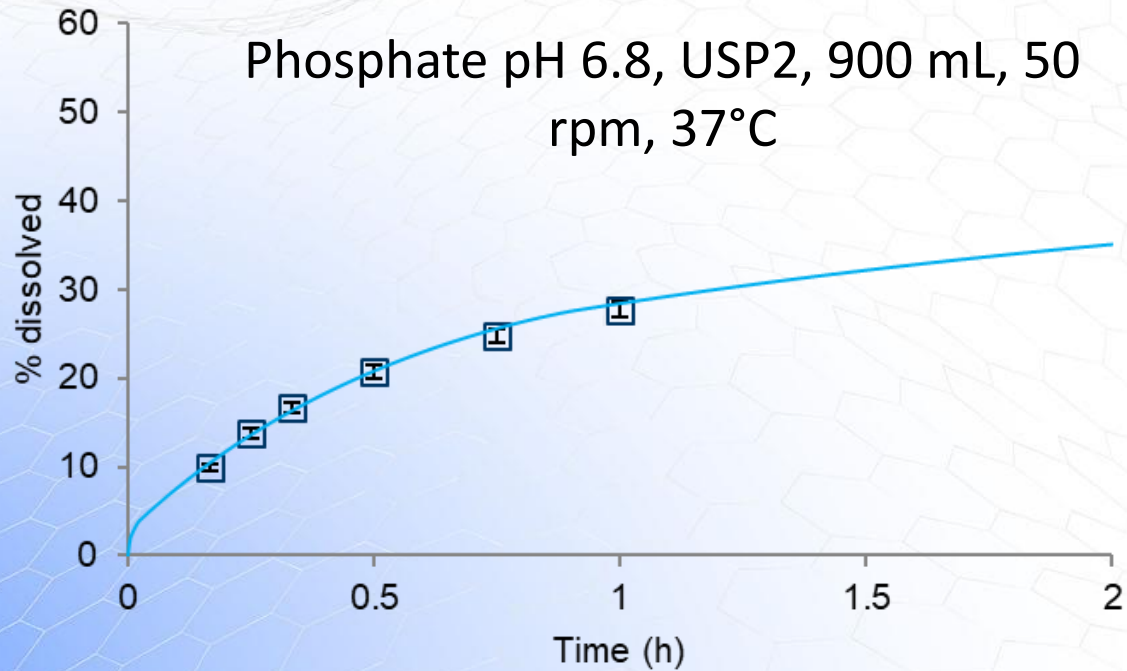
- Data Tab:**
 - Calc Powder surface area m²/g: 0.1530 (Ellipsoid)
 - $C_r = C_s \exp\left(\frac{2\gamma V_m}{rRT}\right)$
 - $\frac{dM_{solid}}{dt} = -S(t) \times \left[f_u \frac{D_u}{h_u(t)} + \frac{D_b}{h_b(t)} \times \frac{1-f_u}{f_u} \right] \times (C_{s,u} - C_u(t))$
- Table Tab:**

Particle size distribution in µm (radii)		
	µm	w/w
r1	1	1.1
r2	2	0.9
r3	10	30.8
r4	20	10.9
r5	30	48.1
r6	50	7.1
r7	60	0.4
r8	70	0.3
r9	80	0.2
r10	90	0.2
		100

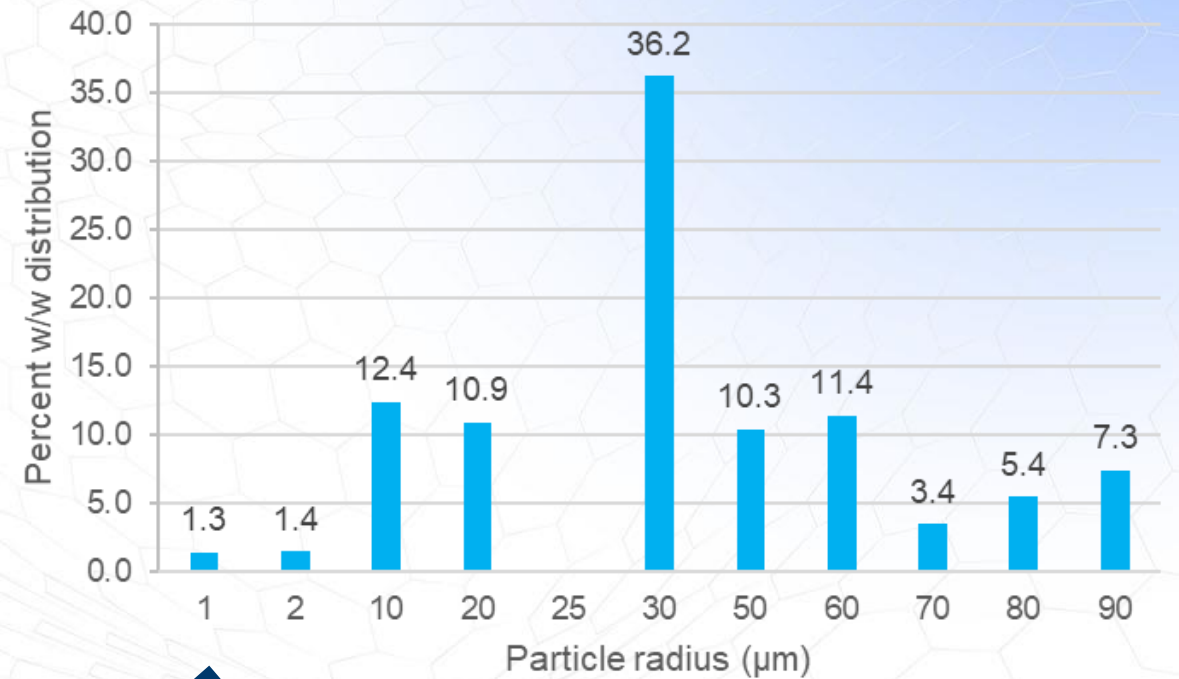
<https://doi.org/10.1016/j.ejpb.2019.07.014>

Example for P-PSD extraction

Step 1 : 100 mg acalabrutinib capsule batch W027180

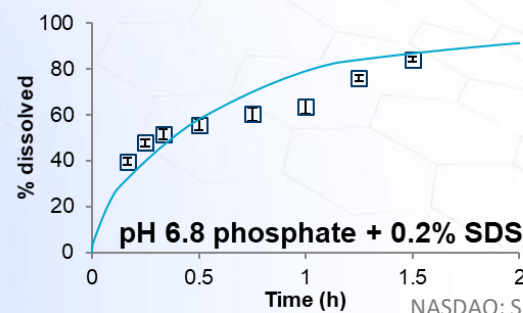
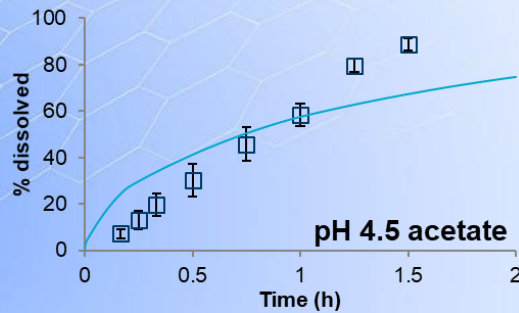
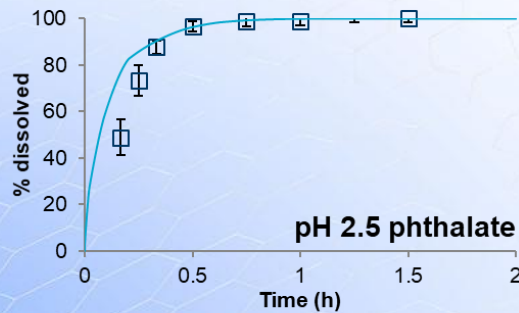
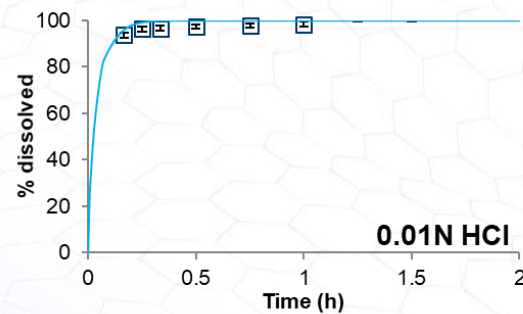
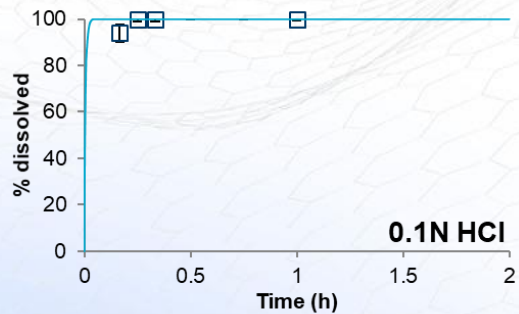


P-PSD for batch W027180



Example for P-PSD verification

Step 2 : Predicting other conditions for 100 mg acalabrutinib capsule batch W027180

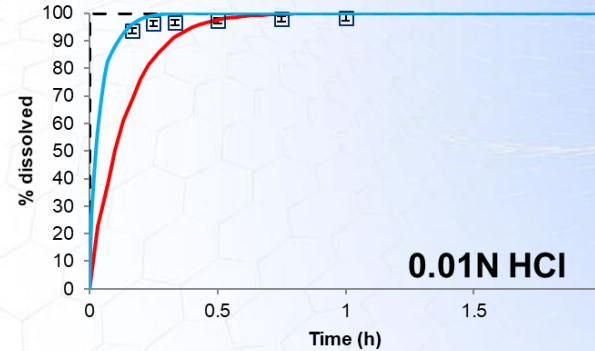
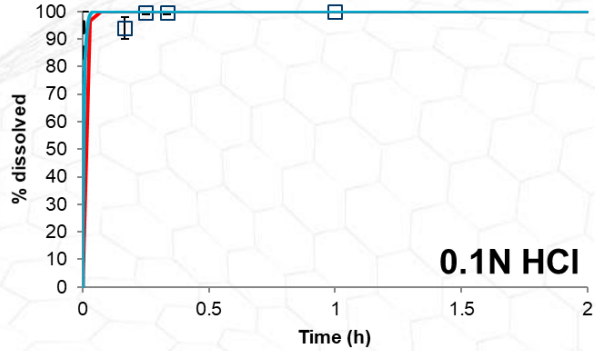


P-PSD able to reproduce the observed dissolution rates in other conditions of pH with and without surfactant

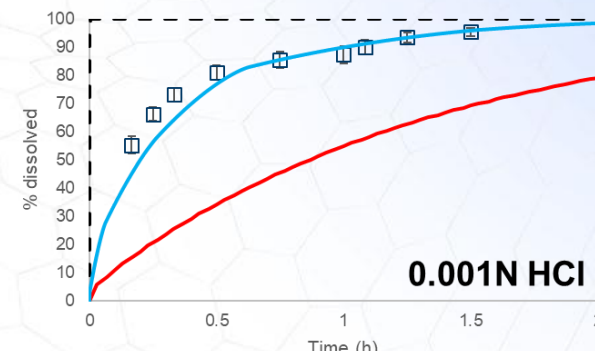
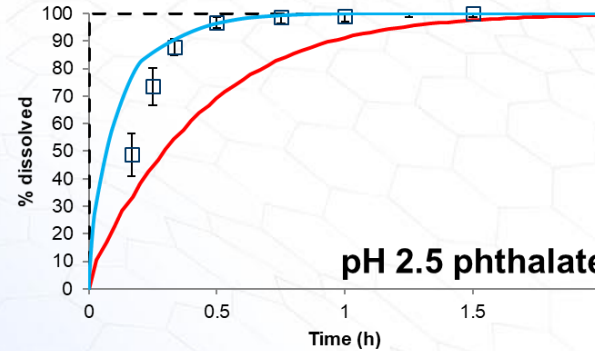
Use of surface pH
Different UWL thicknesses
(if micelles)

Other alternatives to predict dissolution (DS-PSD or bulk solubility)

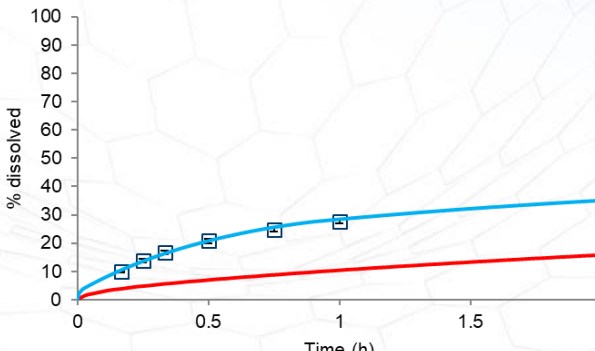
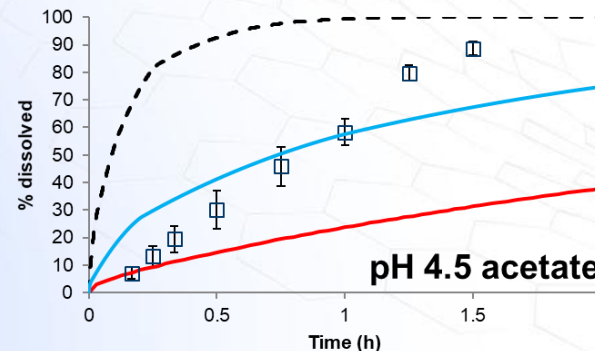
DS-PSD underestimates dissolution



Bulk solubility and P-PSD overestimates dissolution



Surface solubility and P-PSD is the way forward !



100 mg capsule batch
W027180

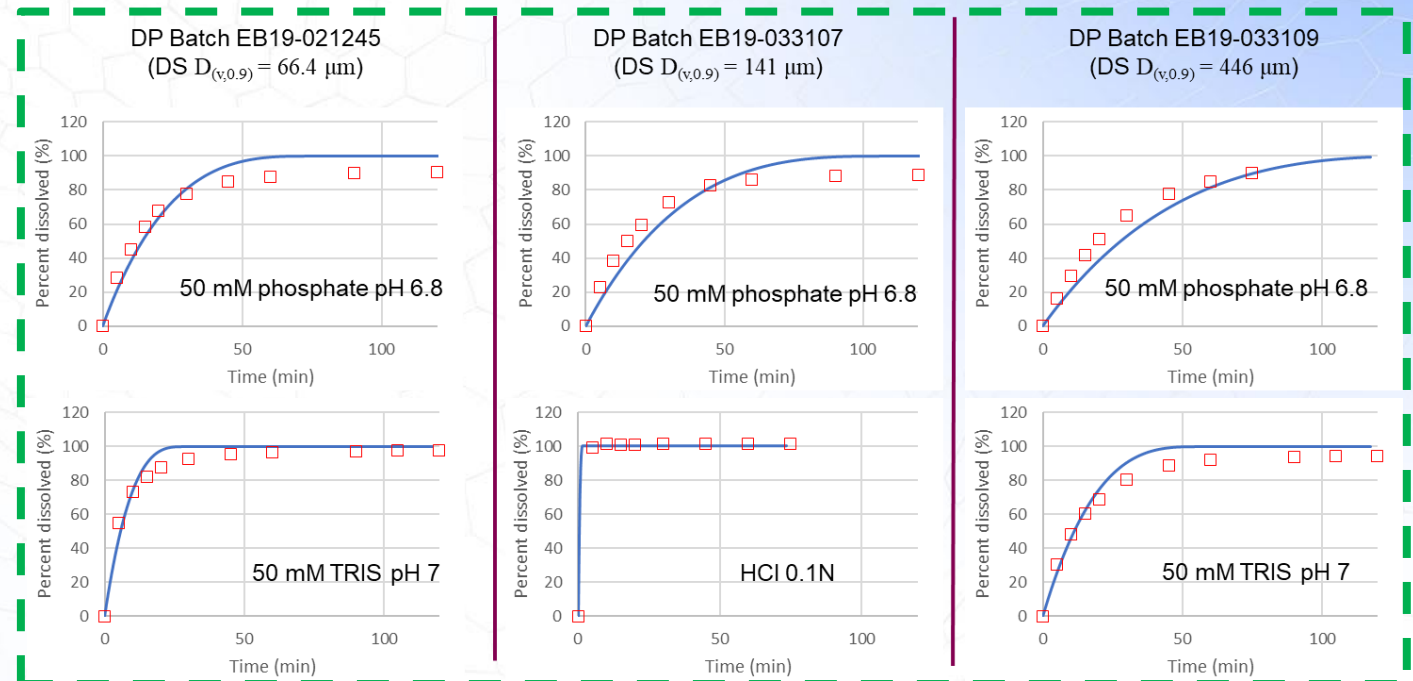
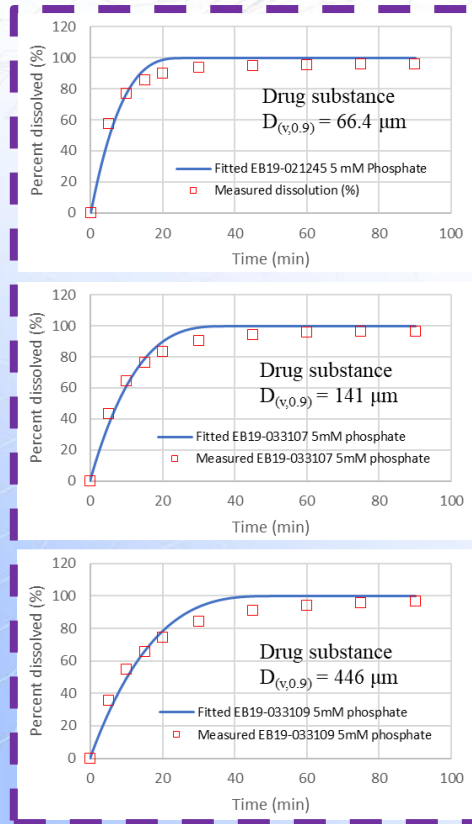
AFE and AAFE : Indicators of goodness of fit

z-factor fitting of dissolution

1-QC dissolution
method + z-factor fit

2-Z-factor verification: dissolution prediction in other media

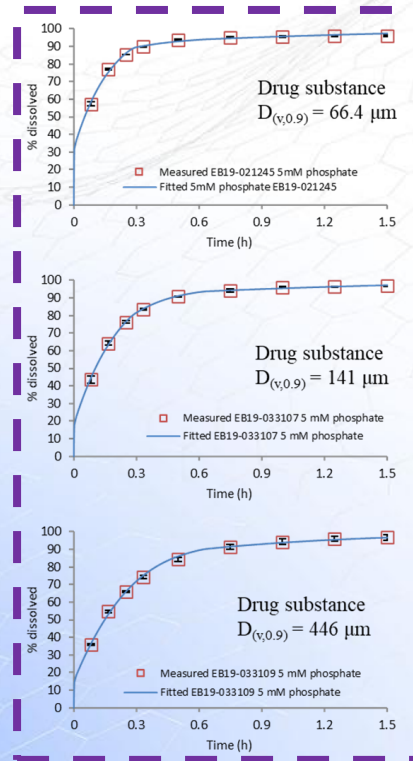
AFE=0.96, AAFE= 1.12



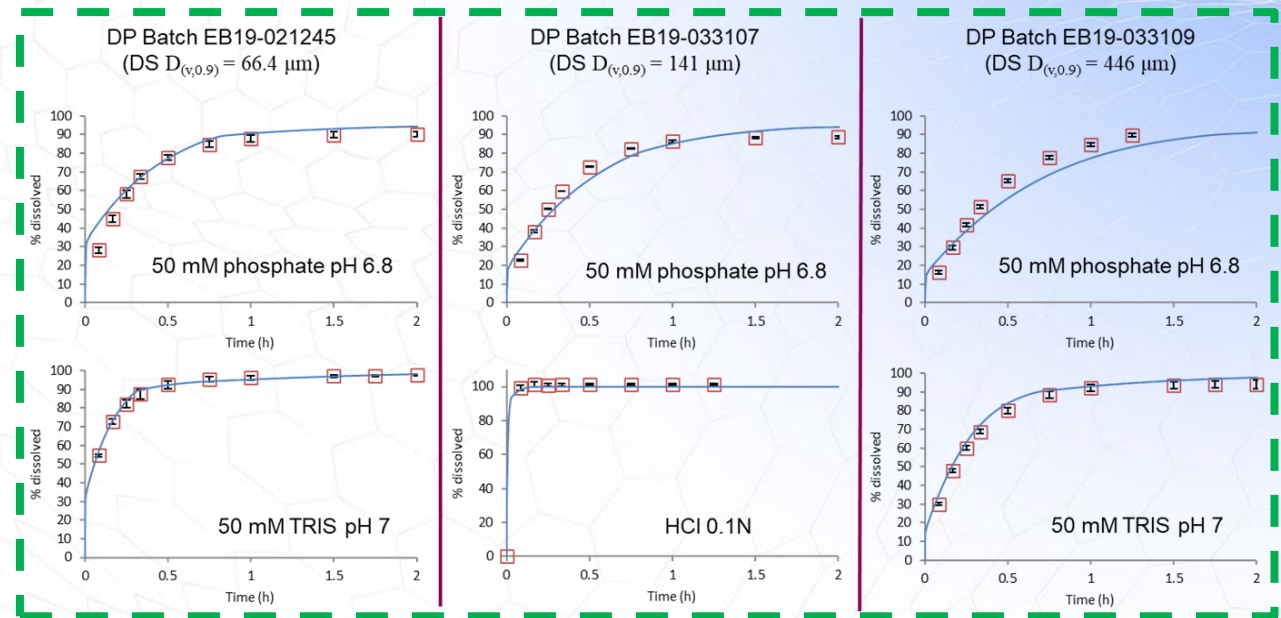
AFE and AAFE : Indicators of goodness of fit P-PSD fitting of dissolution

1-QC dissolution
method + P-PSD extraction

2-P-PSD verification: dissolution prediction in other media




AFE=1.02, AAFE= 1.06



Absolute prediction error during verification
P-PSD = 6% vs z-factor = 12%
P-PSD chosen

Outline

- Different models to fit dissolution
 - Assumptions for each model
 - Use for IR formulation fitting
 - Main equations
- Important drivers of dissolution
 - How DS and DP CQAs can influence shape of profile
- How to choose a dissolution method and how to choose fitting strategy ?
-  Take home messages

Take Home Messages

- DS measured laser diffraction is (generally) a poor predictor of drug product dissolution : Excipients, process, aggregation and shape of DS
- IR DP Dissolution fitting should be mechanistic
 - Translate across populations, prandial states, pH in stomach
 - Provide realistic within and between subject variability during VBE
- Prior to fitting dissolution data verify absence of:
 - Precipitation or degradation
 - Agitation effect
- Use the best fitting method if multiple choices
 - Use surface solubility when appropriate
 - Time correct dissolution data for capsule opening or disintegration times
 - AFE and AAFE can be used to screen and select methods across different dissolution conditions
 - Use a discriminant dissolution method to fit

If present, measure independently and integrate in model

Thanks

